# Model Predictive Control Toolbox™

Getting Started Guide



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Model Predictive Control Toolbox™ Getting Started Guide

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# Introduction

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- "Using the Documentation" on page 1-4
- "Bibliography" on page 1-6

## **Product Overview**

The Model Predictive Control Toolbox<sup>™</sup> product is a collection of software that helps you design, analyze, and implement an advanced industrial automation algorithm. Like other MATLAB® tools, it provides a convenient graphical user interface (GUI) as well as a flexible command syntax that supports customization.

A Model Predictive Control Toolbox controller automates a target system (the *plant*) by combining a prediction strategy and a control strategy. An approximate linear plant model provides the prediction. The control strategy compares predicted plant signals to a set of objectives, then adjusts available actuators to achieve the objectives while respecting the plant constraints. Such constraints can include the physical limits of the actuator, boundaries of safe operation, and lower limits for product quality.

Model Predictive Control Toolbox constraint-tolerance differentiates it from other "optimal control" strategies (e.g., the Linear-Quadratic--Gaussian approach supported in Control System Toolbox<sup>TM</sup> software). The impetus for this is industrial experience suggesting that the drive for profitability often pushes the plant to one or more constraints. The Model Predictive Control Toolbox controller considers such factors explicitly, allowing it to allocate the available plant resources intelligently as the system evolves over time.

Model Predictive Control Toolbox software uses the same powerful linear dynamic modeling tools found in Control System Toolbox software and System Identification Toolbox<sup>™</sup> software. You can use transfer functions, state-space matrices, or a combination of transfer functions and state-space matrices. You can also include delays, which are a common feature of industrial plants.

If you do not have a model but can perform experiments, System Identification Toolbox software can help you to develop a plant model from the data and then design a controller for this plant using the Model Predictive Control Toolbox product.

If you use Simulink® to model your plant, the Model Predictive Control Toolbox product provides a Simulink controller block. For example, you can linearize a nonlinear Simulink model, use the linearized model to build a Model Predictive Control Toolbox controller, and evaluate its ability to control the nonlinear model. If you determine that this controller performs well, you

can implement this control strategy in a real plant using Simulink Coder  $^{\text{\tiny TM}}$  software.

For a list of books on predictive control theory and practice, see "Bibliography" on page 1-6. In particular, Maciejowski [4] illustrates and extends Version 1.0 of the Model Predictive Control Toolbox software. (The command format used in [4] is obsolete in Model Predictive Control Toolbox Version 2.0, however.)

## **Using the Documentation**

If you have limited experience with MATLAB or Model Predictive Control Toolbox software, read this guide first. It shows how to:

- Define your plant using Control System Toolbox modeling tools (LTI transfer function and state space models).
- Derive a linear plant model from a nonlinear Simulink representation.
- Design Model Predictive Control for your plant using mpctool, the graphical user interface (GUI), or special commands.
- Simulate Model Predictive Control performance using mpctool, Simulink, or commands.

If you have experience with an earlier Model Predictive Control Toolbox release, we advise you to read this document to familiarize yourself with the many new features and the new command syntax (the earlier syntax is still available, but the underlying code is no longer supported).

**If you need more details**, see the online documentation. To access it from the MATLAB prompt, type:

doc

When the help dialog box appears, select **Model Predictive Control Toolbox** in the **Contents** pane. This displays a roadmap with links to the available documentation components. Briefly, these are:

- Getting Started. The online version of this document.
- MPC Problem Setup. Mathematical details of the Model Predictive Control Toolbox algorithm and user specifications required for controller design.
- MPC Simulink Library. Describes the Model Predictive Controller Block and its use within Simulink.
- Case-Study Examples. Example toolbox applications.
- The Design Tool. Reference manual for mpctool, the GUI.

- Functions. Reference manual describing each Model Predictive Control Toolbox function (used for controller design and simulation in MATLAB commands and scripts).
- Blocks. Reference manual describing the Model Predictive Control Toolbox blocks (used for controller design and simulation in Simulink).
- Object Reference. Details of the controller object that represents a complete controller design.
- Release Notes. Summarizes major features of this release, known limitations, etc.

#### **Related Products**

MathWorks provides other products that complement and enhance the Model Predictive Control Toolbox functionality. For more information, see www.mathworks.com.

# **Bibliography**

- [1] Allgower, F., and A. Zheng, *Nonlinear Model Predictive Control*, Springer-Verlag, 2000.
- [2] Camacho, E. F., and C. Bordons, *Model Predictive Control*, Springer-Verlag, 1999.
- [3] Kouvaritakis, B., and M. Cannon, *Non-Linear Predictive Control: Theory & Practice*, IEE Publishing, 2001.
- [4] Maciejowski, J. M., *Predictive Control with Constraints*, Pearson Education POD, 2002.
- [5] Prett, D., and C. Garcia, *Fundamental Process Control*, Butterworths, 1988.
- [6] Rossiter, J. A., Model-Based Predictive Control: A Practical Approach, CRC Press, 2003.

# **Building Models**

- "Overview" on page 2-2
- "Linear, Time Invariant (LTI) Models" on page 2-4
- "Using System Identification Toolbox Models" on page 2-23
- "Bibliography" on page 2-29

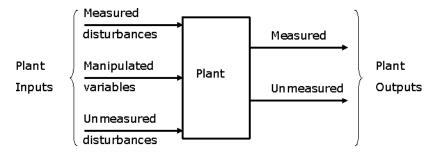
#### **Overview**

This section covers the following topics:

- "Plant Model" on page 2-2
- "Plant Inputs and Outputs" on page 2-3

#### **Plant Model**

The *plant* is the system (process or device) you intend to control. The following figure shows a schematic example.



#### **Plant with Input and Output Signals**

A Model Predictive Control Toolbox design requires a *plant model*, which defines the mathematical relationship between the plant inputs and outputs. The controller uses it to predict plant behavior.

The toolbox software requires the model to be linear, time invariant (LTI). You can define such a model as follows:

- Create a transfer function, state space, or zero/pole/gain model using methods provided by the Control System Toolbox software
- Derive it from plant data using, e.g., methods provided by System Identification Toolbox software
- Derive it by linearizing a Simulink model

This chapter illustrates each of these approaches. Control System Toolbox, Simulink, and System Identification Toolbox documentation provides additional examples and details.

## Plant Inputs and Outputs

#### Inputs

The *plant inputs* are the independent variables affecting the plant. As shown in Plant with Input and Output Signals on page 2-2, there are three types:

**Measured disturbances.** The controller can't adjust them, but uses them for feedforward compensation.

**Manipulated variables.** The controller adjusts these in order to achieve its goals.

**Unmeasured disturbances.** These are independent inputs of which the controller has no direct knowledge, and for which it must compensate.

#### **Outputs**

The *plant outputs* are the dependent variables (outcomes) you wish to control or monitor. As shown in Plant with Input and Output Signals on page 2-2, there are two types:

**Measured outputs.** The controller uses these to estimate unmeasured quantities and as feedback on the success of its adjustments.

**Unmeasured outputs.** The controller estimates these based on available measurements and the plant model. The controller can also hold unmeasured outputs at setpoints or within constraint boundaries.

You must specify the input and output types when designing the controller. See "Input and Output Types" on page 2-9 for more details.

## Linear, Time Invariant (LTI) Models

Model Predictive Control Toolbox software supports the same LTI model formats as does Control System Toolbox software. You can use whichever is most convenient for your application. It's also easy to convert from one format to another.

The following sections describe the three model formats and the commands used to construct them:

- "Transfer Function Format" on page 2-4
- "Zero/Pole/Gain Format" on page 2-5
- "State-Space Format" on page 2-5
- "LTI Object Properties" on page 2-7
- "Multiinput-Multioutput (MIMO) Plants" on page 2-11
- "LTI Model Characteristics" on page 2-13

For more details, see the Control System Toolbox documentation.

### **Transfer Function Format**

A transfer function (TF) relates a particular input/output pair. For example, if u(t) is a plant input and y(t) is an output, the transfer function relating them might be:

$$\frac{Y(s)}{U(s)} = G(s) = \frac{s+2}{s^2 + s + 10}e^{-1.5s}$$

This TF consists of a *numerator* polynomial, s+2, a *denominator* polynomial,  $s^2+s+10$ , and a delay, which is 1.5 time units here. You can define G using Control System Toolbox tf function:

Control System Toolbox software builds and displays it as follows:

Transfer function:

### **Zero/Pole/Gain Format**

Like the TF, the zero/pole/gain (ZPK) format relates an input/output pair. The difference is that the ZPK numerator and denominator polynomials are factored, as in

$$G(s) = 2.5 \frac{s + 0.45}{(s + 0.3)(s + 0.1 + 0.7i)(s + 0.1 - 0.7i)}$$

(zeros and/or poles are complex numbers in general).

You define the ZPK model by specifying the zero(s), pole(s), and gain as in

$$Gzpk1 = zpk(-0.45, [-0.3, -0.1+0.7*i, -0.1-0.7*i], 2.5)$$

## **State-Space Format**

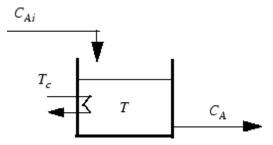
#### **Chemical Reactor Example**

The state-space format is convenient if your model is a set of LTI differential and algebraic equations. For example, consider the following linearized model of a continuous stirred-tank reactor (CSTR) involving an exothermic (heat-generating) reaction [9]

$$\frac{dC_A'}{dt} = a_{11}C_A' + a_{12}T' + b_{11}T_c' + b_{12}C_{Ai}'$$

$$\frac{dT'}{dt} = a_{21}C'_A + a_{22}T' + b_{21}T'_c + b_{22}C'_{Ai}$$

where  $C_A$  is the concentration of a key reactant, T is the temperature in the reactor,  $T_c$  is the coolant temperature,  $C_{Ai}$  is the reactant concentration in the reactor feed, and  $a_{ij}$  and  $b_{ij}$  are constants. See the process schematic in CSTR Schematic on page 2-6. The primes (e.g.,  $C_A$ ) denote a deviation from the nominal steady-state condition at which the model has been linearized.



#### **CSTR Schematic**

Measurement of reactant concentrations is often difficult, if not impossible. Let us assume that T is a measured output,  $C_A$  is an unmeasured output,  $T_c$  is a manipulated variable, and  $C_{Ai}$  is an unmeasured disturbance.

#### **State-Space Format**

The model fits the general state-space format

$$\frac{dx}{dt} = Ax + Bu$$

$$y = Cx + Du$$

where

$$x = \begin{bmatrix} C_A' \\ T' \end{bmatrix} u = \begin{bmatrix} T_c' \\ C_{Ai}' \end{bmatrix} y = \begin{bmatrix} T' \\ C_A' \end{bmatrix},$$

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \quad B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} C = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} D = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

The following code shows how to define such a model for some specific values of the  $a_{ij}$  and  $b_{ij}$  constants:

This defines a *continuous-time* state-space model. If you do not specify a sampling period, a default sampling value of zero applies. You can also specify discrete-time state-space models. You can specify delays in both continuous-time and discrete-time models. For more information, see the Control System Toolbox documentation.

**Note** In the CSTR example, the D matrix is zero and the output does not instantly respond to change in the input. The Model Predictive Control Toolbox software prohibits direct (instantaneous) feedthrough from a manipulated variable to an output. For example, the CSTR model could include direct feedthrough from the unmeasured disturbance,  $C_{Ai}$ , to either  $C_A$  or T but direct feedthrough from  $T_c$  to either output would violate this restriction. If the model had direct feedthrough from  $T_c$ , you could have added a small delay at this input to circumvent the problem.

## **LTI Object Properties**

The ss function in the last line of the above code creates a state space model, CSTR, which is an LTI object. The tf and zpk commands described in "Transfer Function Format" on page 2-4 and "Zero/Pole/Gain Format" on page 2-5 also create LTI objects. Such objects contain the model parameters as well as optional properties.

#### LTI Properties for the CSTR Example

The following code sets some of the CSTR model's optional properties:

```
CSTR.InputName = {'T_c', 'C_A_i'};
CSTR.OutputName = {'T', 'C_A'};
CSTR.StateName = {'C_A', 'T'};
CSTR.InputGroup.MV = 1;
CSTR.InputGroup.UD = 2;
CSTR.OutputGroup.W0 = 1;
CSTR.OutputGroup.UO = 2;
```

#### **CSTR**

The first three lines specify labels for the input, output and state variables. The next four specify the signal type for each input and output. The designations MV, UD, MO, and UO mean manipulated variable, unmeasured disturbance, measured output, and unmeasured output. (See "Plant Inputs and Outputs" on page 2-3 for definitions.) For example, the code specifies that input 2 of model CSTR is an unmeasured disturbance. The last line causes the LTI object to be displayed, generating the following lines in the MATLAB Command Window:

Output groups: Name

Channels

MO 1 U0 2

Continuous-time model

#### **Input and Output Names**

The optional InputName and OutputName properties affect the model displays, as in the above example. The toolbox also uses the InputName and OutputName properties to label plots and tables. In that context, the underscore character causes the next character to be displayed as a subscript.

#### **Input and Output Types**

**General Case.** As mentioned in "Overview" on page 2-2, Model Predictive Control Toolbox software supports three input types and two output types. In a Model Predictive Control Toolbox design, designation of the input and output types determines the controller dimensions and has other important consequences.

For example, suppose your plant structure were as follows.

Plant Inputs	Plant Outputs
Two manipulated variables (MVs)	Three measured outputs (MOs)
One measured disturbance (MD)	Two unmeasured outputs (UOs)
Two unmeasured disturbances (UDs)	

The resulting controller would have four inputs (the three MOs and the MD) and two outputs (the MVs). It would include feedforward compensation for the measured disturbance, and would assume that you wanted the unmeasured disturbances and outputs to be included as part of the regulator design.

If you didn't want a particular signal to be treated as one of the above types, you could do one of the following:

• Eliminate the signal before using the model in controller design.

- For an output, designate it as unmeasured, then set its weight to zero (see "Output Weights" on page 3-22).
- For an input, designate it as an unmeasured disturbance, then define a custom state estimator that ignores the input (see "Disturbance Modeling and Estimation" on page 3-31).

**Note** By default, the toolbox assumes that unspecified plant inputs are manipulated variables, and unspecified outputs are measured. Thus, if you didn't specify signal types in the above example, the controller would have four inputs (assuming all plant outputs were measured) and five outputs (assuming all plant inputs were manipulated variables).

**Example.** For model CSTR, default Model Predictive Control Toolbox assumptions are incorrect. You must set its InputGroup and OutputGroup properties, as illustrated in the above code, or modify the default settings when you load the model into the design tool.

The toolbox provides a "helper" function called setmpcsignals to make type definition more convenient. For example

```
CSTR = setmpcsignals(CSTR, 'UD', 2, 'UO', 2);
```

sets InputGroup and OutputGroup to the same values as in the previous example. The CSTR display would then include the following lines:

#### Input groups:

Name	Channels
Unmeasured	2
Manipulated	1

#### Output groups:

Name	Channels
Unmeasured	2
Measured	1

Notice that setmpcsignals sets unspecified inputs to Manipulated and unspecified outputs to Measured.

See the Control System Toolbox documentation for additional information on LTI object properties.

## Multiinput-Multioutput (MIMO) Plants

Most Model Predictive Control Toolbox applications involve plants having multiple inputs and outputs. Model CSTR described in "State-Space Format" on page 2-5 is a MIMO plant, and the state space format extends naturally from single-input single-output (SISO) to MIMO plants.

You can also use the tf and zpk functions to build a MIMO plant model. For example, consider the following model of a distillation column [11], which has been used in many advanced control studies:

$$\begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} \frac{12.8e^{-s}}{16.7s + 1} & \frac{-18.9e^{-3s}}{21.0s + 1} & \frac{3.8e^{-8.1s}}{14.9s + 1} \\ \frac{6.6e^{-7s}}{10.9s + 1} & \frac{-19.4e^{-3s}}{14.4s + 1} & \frac{4.9e^{-3.4s}}{13.2s + 1} \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

Outputs  $y_1$  and  $y_2$  represent measured product purities. The control objective is to hold each at specified setpoints. To do so, the controller manipulates inputs  $u_1$  and  $u_2$ , the flow rates of reflux and reboiler steam, respectively. Input  $u_3$  is a measured feed flow rate disturbance.

The model consists of six transfer functions, one for each input/output pair. Each transfer function is the first-order-plus-delay form often used by process control engineers.

The following code shows how to define the distillation column model for use in the toolbox:

```
g11 = tf( 12.8, [16.7 1], 'IOdelay', 1.0);
g12 = tf(-18.9, [21.0 1], 'IOdelay', 3.0);
g13 = tf( 3.8, [14.9 1], 'IOdelay', 8.1);
g21 = tf( 6.6, [10.9 1], 'IOdelay', 7.0);
g22 = tf(-19.4, [14.4 1], 'IOdelay', 3.0);
```

The code defines the individual transfer functions, and then forms a matrix in which each row contains the transfer functions for a particular output, and each column corresponds to a particular input. The code also sets the signal names and designates the third input as a measured disturbance. The resulting LTI object display is as follows:

```
Transfer function from input "Reflux Rate" to output...
                                  12.8
Distillate Purity: exp(-1*s) * ------
                               16.7 s + 1
Bottoms Purity: exp(-7*s) * ------
                            10.9 s + 1
Transfer function from input "Steam Rate" to output...
Distillate Purity: exp(-3*s) * -----
                               21 s + 1
Bottoms Purity: exp(-3*s) * ------
                            14.4 s + 1
Transfer function from input "Feed Rate" to output...
Distillate Purity: exp(-8.1*s) * ------
                                 14.9 s + 1
Bottoms Purity: exp(-3.4*s) * ------
                             13.2 s + 1
Input groups:
```

Name Channels Measured 3 Manipulated 1,2

Output groups:

Name Channels Measured 1,2

### **LTI Model Characteristics**

Control System Toolbox software provides functions for analyzing LTI models. Some of the more commonly used are listed below. Type the example code at the MATLAB prompt to see how they work for the CSTR example.

Example	Intended Result
dcgain(CSTR)	Calculate gain matrix for the CSTR model's input/output pairs.
impulse(CSTR)	Graph CSTR model's unit-impulse response.
ltiview(CSTR)	Open the LTI Viewer with the CSTR model loaded. You can then display model characteristics by making menu selections.
pole(CSTR)	Calculate CSTR model's poles (to check stability, etc.).
step(CSTR)	Graph CSTR model's unit-step response.
zero(CSTR)	Compute CSTR model's transmission zeros.

## **Using Simulink Control Design to Linearize Simulink Model**

The LTI models discussed in the previous sections are *linear* dynamic models. Most real systems are nonlinear. If you'd like to simulate Model Predictive Control Toolbox control of a nonlinear system, you must model the plant in Simulink.

Although a Model Predictive Control Toolbox controller can regulate a nonlinear plant, the model used within the controller must be linear. In other words, the controller employs a linear approximation of the nonlinear plant. The accuracy of this approximation is a key issue affecting controller performance.

This raises the question: how to obtain the approximation? The usual approach is to *linearize* the nonlinear plant at a specified *operating point*. The Simulink environment provides two ways to accomplish this:

- "Linearization Using MATLAB Code" on page 2-14
- "Linearization Using Linear Analysis Tool in Simulink Control Design" on page 2-17

### **Linearization Using MATLAB Code**

This example shows how to obtain a linear model of a plant using commands.

Linearize the CSTR model. For this model, the controller will adjust a coolant temperature, which is one of three plant inputs. The others are the concentration of the limiting reactant in the CSTR feed stream and the temperature of this stream. The CSTR states are the temperature and concentration of the limiting reactant in the product stream. We will assume that both can be measured and used for feedback control.

**1** Determine an operating point.

The operating point defines the nominal conditions at which you will linearize. It is usually a steady state.

Suppose you plan to operate the CSTR with the output concentration at 2 kmol/m<sup>3</sup>. The nominal feed concentration is 10 kmol/m<sup>3</sup> and the nominal

feed temperature is 300 K. Create an operating point specification object to define the steady state.

```
opspec = operspec('CSTR_OpenLoop');
opspec = addoutputspec(opspec,'CSTR_OpenLoop/CSTR',2);
opspec.Outputs(1).Known = true;
opspec.Outputs(1).y = 2;
```

The use findop to compute the steady state (trimming)

```
op1 = findop('CSTR OpenLoop',opspec);
```

The calculated operating point is  $C_A = 2 \text{ kmo1/m}^3$  and  $T_K = 373 \text{ K}$ . Notice that the coolant temperature at steady state is also given as 299 K, which is the nominal value of the manipulated variable of the model predictive controller.

In another example, suppose you plan to operate the CSTR with coolant temperature fixed at 305K. You can compute the new operating point with the following specification:

```
opspec = operspec('CSTR_OpenLoop');
opspec.States(1).x = 1;
opspec.States(2).x = 400;
opspec.Inputs(1).Known = true;
opspec.Inputs(1).u = 305;
```

Again, use findop to compute the steady state (trimming).

```
op2 = findop('CSTR_OpenLoop',opspec);
```

The calculated operating point is  $C_A = 1.78 \text{ kmol/m}^3$  and  $T_K = 377 \text{ K}$ . Notice that we provide an initial guess of  $C_A$  and  $T_K$  in the specification due to strong nonlinearity in the CSTR plant.

**2** Designate the desired input and output signals.

Specify all three inputs and the two outputs as follows:

```
io(1) = linio('CSTR_OpenLoop/Feed Concentration', 1, 'in');
io(2) = linio('CSTR_OpenLoop/Feed Temperature', 1, 'in');
```

```
io(3) = linio('CSTR_OpenLoop/CoolantTemperature', 1, 'in');
io(4) = linio('CSTR_OpenLoop/CSTR', 1, 'out');
io(5) = linio('CSTR OpenLoop/CSTR', 2, 'out');
```

If the input and output signals are already defined in the Simulink model, e.g. as in the CSTR\_OpenLoop example, use the following to get the signals:

```
io = getlinio('CSTR OpenLoop');
```

**3** Linearize at the chosen operating point.

Use linearize as follows to linearize the plant at the steady state operating point op1:

```
sys = linearize('CSTR OpenLoop', op1, io)
```

where sys is a continuous-time state space model with the following parameters:

```
a =
                       t k
             са
              - 5
                  -0.3427
   c_a
                    2.785
           47.68
   t_k
b =
        coolant temp
                       feed concent feed tempera
   c_a
                                    1
                  0.3
                                    0
                                                   1
   t_k
c =
            c_a t_k
              0
   cstr/1
   cstr/2
              1
                   0
d =
                          feed concent
                                          feed tempera
            coolant temp
   cstr/1
                        0
                                       0
                                                      0
   cstr/2
                        0
                                       0
                                                      0
```

The linearized model has three inputs and two outputs, as expected. The input sequence is: Coolant Temperature, Feed Concentration and Feed Temperature. The output sequence is CSTR/1 = T\_K (reactor temperature) and CSTR/2 = C A (reactant concentration).

# Linearization Using Linear Analysis Tool in Simulink Control Design

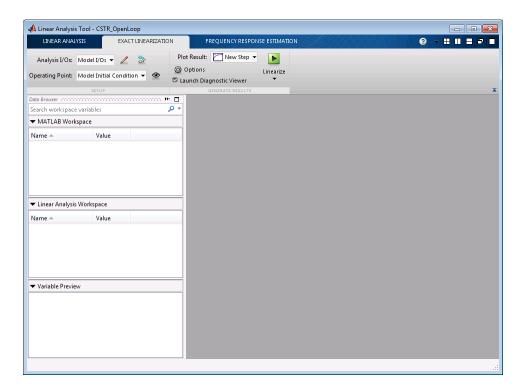
The Linear Analysis Tool provided by Simulink Control Design™ is a graphical interface for model linearization.

This example shows how to linearize a Simulink model using the Linear Analysis Tool.

1 Open the Simulink model.

```
sys = 'CSTR_OpenLoop.mdl';
open system(sys)
```

2 In the Simulink model window, select Tools > Control Design > Linear Analysis.



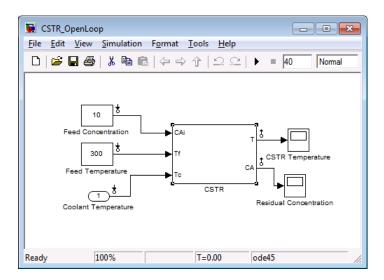
This action opens the Linear Analysis Tool for the model.

- 3 Select linearization input signals.
  - In the Simulink model window, right-click the output signal from the Feed Concentration block. Select Linearization Points > Input Point.
  - In the Simulink model window, right-click the output signal from the Feed Temperature block. Select Linearization Points > Input Point.
  - In the Simulink model window, right-click the output signal from the Coolant Temperature block. Select Linearization Points > Input Point.

Select linearization output signals.

•

- In the Simulink model window, right-click the input signal to the CSTR Temperature block. Select Linearization Points > Output Point.
- In the Simulink model window, right-click the input signal to the Residual Concentration block. Select Linearization Points > Output Point.



The above actions add linearization input and output signals to the model.

- **4** In the Simulink model window, right-click the CA output signal from the CSTR block. Select **Linearization Points > Output Constraint**.
- 5 Click the Exact Linearization tab of the Linear Analysis Tool. In the Operating Point drop-down list, select Trim model....

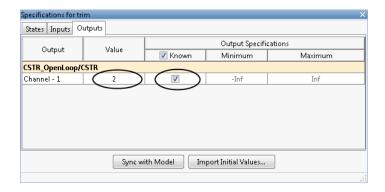
This action opens the **Trim Model** tab.

Click **Specifications**.

This action opens the **Specifications for trim** dialog box.

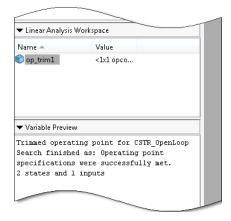
6 Select the Outputs tab and set the value of the CSTR\_OpenLoop/CSTR (CA) to 2 kmol/m<sup>3</sup>.

Select the **Known** check box.



#### 7 In the Trim Model tab, click Trim.

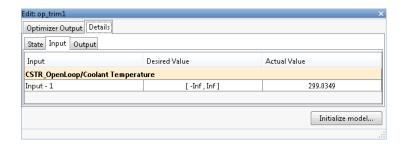
This action creates the operating point op\_trim1 in the Linear Analysis Workspace.



Double click op\_trim1.

This action opens the Edit trim point dialog box.

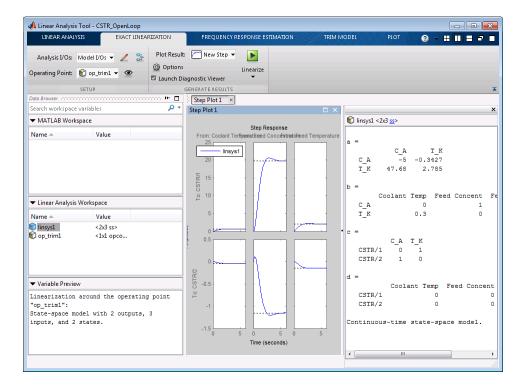
Select the **Input** tab.



The coolant temperature at steady state is 299 K, as desired.

- 8 In the Exact Linearization tab, select op\_trim1 from the Operating Point list.
- 9 Click Linearize.

This action creates the linear model linsys1 in the Linear Anaysis Workspace. linsys1 uses op\_trim1 as its operating point.



The step response from feed concentration to output CSTR/2 displays an interesting inverse response. An examination of the linear model shows that CSTR/2 is the residual CSTR concentration, C\_A. When the feed concentration increases, C\_A increases initially (more reactant is entering), which increases the reaction rate. This increases the reactor temperature (output CSTR/1), which further increases the reaction rate and C\_A decreases dramatically.

**10** Export the linearization result to the MATLAB workspace.

If necessary, you can repeat any of the above steps. Once you are satisfied with your linear model, drag and drop it from the **Linear Anaysis Workspace** to the **MATLAB Workspace** in the Linear Analysis Tool.
You may now use the linearization result with other tools, such as the controller design.

# **Using System Identification Toolbox Models**

#### In this section...

"Estimate Plant Model" on page 2-23

"Construct Model Predictive Controller with System Identification Toolbox Model" on page 2-24

"How Inputs are Treated" on page 2-26

"Using Step-Response Models" on page 2-27

#### **Estimate Plant Model**

System Identification Toolbox software generates LTI models based on plant input/output data. To use System Identification Toolbox software, you first create an iddata object containing measured values of your plant input and output signals.

**Note** The System Identification Toolbox product is optional. To determine whether your installation includes it, type ver at the MATLAB prompt, and look for "System Identification Toolbox" in the list of installed products.

The following example uses the System Identification Toolbox tutorial data set, a temperature-control application. Load the data as follows:

load dryer2

This creates vectors u2 and y2 in your workspace. Vector u2 is a sequence of 1000 plant input values (electrical power), and y2 is the corresponding output sequence (1000 temperature values). The sampling period is 0.08 second.

Create an iddata object called dry as follows:

```
dry = iddata(y2,u2,0.08);
```

Once the data has been loaded, use the System Identification Toolbox GUI or commands to determine a model that best fits the data. For example, the commands

```
dry.InputName = 'Power';
dry.OutputName = 'Temperature';
ze = detrend(dry);
m1 = pem(ze);
```

create a System Identification Toolbox model called m1 (see the System Identification Toolbox documentation for a detailed explanation). If you type

```
whos m1
```

at the MATLAB prompt, the displayed result is:

Name	Size	Bytes Class
m 1	4 - D	22470 idss object

Notice that m1 is an idss object, one of several possible System Identification Toolbox model types (idgrey, idarx, idpoly, idproc, idss, idmodel, idtf and idfrd). The pem function settings govern the type of model generated.

Like other System Identification Toolbox objects, m1 defines a model structure and adjustable parameter values that best fit the data. It also contains toolbox-specific information, such as the algorithm used to estimate the parameters.

# Construct Model Predictive Controller with System Identification Toolbox Model

After creating a System Identification Toolbox model based on your data, create a model predictive controller using one of the following methods:

- Use mpc to create the model predictive controller with the System Identification Toolbox model as the plant input argument. mpc will automatically convert the plant input to an ss model.
- First, manually convert the System Identification Toolbox model to an ss model. Then, use mpc to create a model predictive controller using the resulting ss model as the input argument.

Use the ss function to convert a System Identification Toolbox model object (except the idfrd type) to a standard Control System Toolbox

ss (state-space) object, which is the form used internally by the Model Predictive Control Toolbox software. For example,

```
m1ss = ss(m1)
```

converts m1, a System Identification Toolbox object, to m1ss, an LTI ss object, and displays the following:

a = х1 х2 хЗ 0.9492 -0.2127 0.03679 х1 х2 0.2599 0.6523 0.2342 хЗ -0.04822 -0.6639 0.1393

c = x1 x2

Temperature 14.09 -0.108 -0.08164

d =

Power v@Temperatur
Temperature 0 0.03968

Input groups:

Name Channels Measured 1 Noise 2

Sampling time: 0.08 Discrete-time model

Here m1ss is a third-order, discrete-time, state-space model with a sampling time of 0.08, one output (Temperature), and two inputs (Power and v@Temperatur).

х3

For information regarding how the inputs of the generated state-space model are handled by the MPC controller, see "How Inputs are Treated" on page 2-26.

# **How Inputs are Treated**

The software adds a noise input to your system for each output when converting the System Identification Toolbox model object to an ss object.

For example, the software adds the noise input v@Temperatur for the output signal Temperature that is associated with m1ss. This noise signal models the impact of unmeasured disturbances and measurement noise. The InputGroup property of the ss object for the added noise signals is Noise. All other inputs of the ss object are placed in the Measured input group.

When creating the controller, mpc treats the measured inputs of the ss object differently than the noise inputs. By default:

- for measured inputs, mpc treats these signals as manipulated variables
- for noise inputs, mpc treats these signals as unmeasured input disturbances. That is, the columns of the B matrix related to noise inputs are treated as the effect of unmeasured input disturbances on the state of the plant. Similarly, the columns of the D matrix related to noise inputs are treated as the effect of unmeasured input disturbances on the output of the plant

If these signal default values are inappropriate, you must correct them prior to using the model in a design:

- Use setmpcsignals to set the signal types for an LTI plant model.
- If you are using the design tool, see "Signal Property Specifications" on page 3-5 for information on specifying signal types.

**Note** As discussed in "Disturbance Modeling and Estimation" on page 3-31, unmeasured input disturbances influence the default controller design. A System Identification Toolbox model of its Noise inputs might fit the given data, but another experiment might yield a very different noise model. If a controller designed using such a model seems to work well during setpoint changes but is slow to eliminate disturbances or exhibits steady-state error, try modifying the Model Predictive Control Toolbox disturbance modeling settings.

# **Using Step-Response Models**

Early predictive control implementations used finite step-response or finite impulse-response models, often called *nonparametric* LTI models (see [6] for example). Such models are easy to determine from plant data ([3], [7]) and they have intuitive appeal.

System Identification Toolbox software includes tools for nonparametric model identification. See the System Identification Toolbox documentation for details.

For example, given the iddata object ze (defined in "Estimate Plant Model" on page 2-23), you could type:

```
m2 = step(ze);
```

This identifies a finite step-response model, m2, which is a System Identification Toolbox idarx object. Then typing

```
step(m2)
```

would display its unit-step response.

You could convert m2 to an LTI object for use in the Model Predictive Control Toolbox design as a plant (see "Construct Model Predictive Controller with System Identification Toolbox Model" on page 2-24). The disadvantage is that the model will be high-order, especially if your plant is MIMO. For example, converting m2 generates an ss object of order 69.

High-order models can degrade certain Model Predictive Control Toolbox operations, such as estimator design. As is the case with most recent predictive control implementations (see [5] for example), Model Predictive Control Toolbox algorithms work best with a low-order parametric model. For example, reference [10] describes a systematic approach that identifies a step-response model as an intermediate step. The System Identification Toolbox documentation also advocates this approach.

# **Bibliography**

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- [10] Wang, L., P. Gawthrop, C. Chessari, T. Podsiadly, and A. Giles, "Indirect approach to continuous time system identification of food extruder," *J. Process Control*, Vol. 14, Number 6, pp. 603–615, 2004.
- [11] Wood, R. K., and M. W. Berry, Chem. Eng. Sci., Vol. 28, pp. 1707, 1973.

# Designing Controllers Using the Design Tool GUI

- "Introduction" on page 3-2
- "Linear Simulations" on page 3-11
- "Changing Controller Settings" on page 3-19
- "Defining Soft Output Constraints" on page 3-39
- "Robustness Testing" on page 3-43
- "Plant Models with Delays" on page 3-46
- "Nonsquare Plants" on page 3-51
- "Nonlinear Plants" on page 3-53
- "Saving Your Work" on page 3-65
- "Loading Your Saved Work" on page 3-68

# Introduction

The Model Predictive Control Toolbox design tool is a graphical user interface for controller design. This GUI is part of the Control and Estimation Tools Manager GUI. To learn about using the Control and Estimation Tools Manager for linearization, see "Linearization Using Linear Analysis Tool in Simulink Control Design" on page 2-17.

This section covers the following topics:

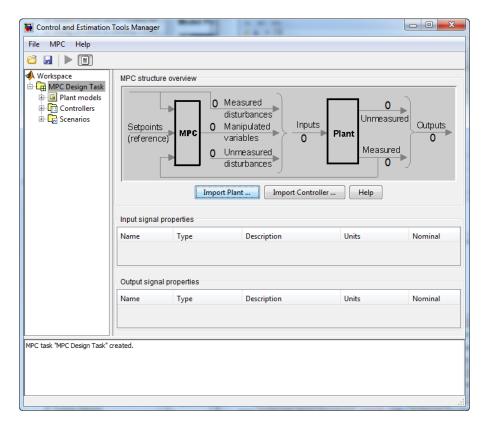
- "Starting the Design Tool" on page 3-2
- "Loading a Plant Model" on page 3-3
- "Signal Property Specifications" on page 3-5

#### **Starting the Design Tool**

Start the design tool by typing the MATLAB command

mpctool

The Control and Estimation Tools Manager window appears, as shown below. By default, it contains a Model Predictive Control Toolbox task called **MPC Design Task** (listed in the tree view on the left side of the window), which is selected, causing the view shown on the right to appear.



Model Predictive Control Toolbox Design Tool Initial View

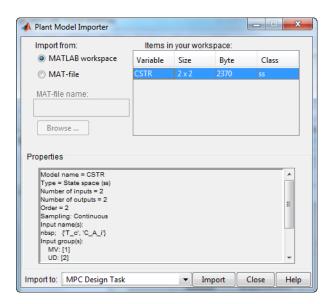
# **Loading a Plant Model**

The first step in the design is to load a plant model. Its dimensions and signal characteristics set the context for the remaining steps. You can either load the model directly, as described in this section, or indirectly by importing a controller or a saved design (see "Loading Your Saved Work" on page 3-68).

The following example uses the CSTR model described in "State-Space Format" on page 2-5. Verify that the LTI object CSTR is in your MATLAB workspace (if necessary, create the model as explained in "State-Space Format" on page 2-5, and set its label and signal type properties as explained in "LTI Object Properties" on page 2-7).

#### **Plant Model Importer Dialog Box**

Click the **Import Plant** button in the design tool's initial view (see Model Predictive Control Toolbox Design Tool Initial View on page 3-3). The Plant Model Importer dialog box appears.

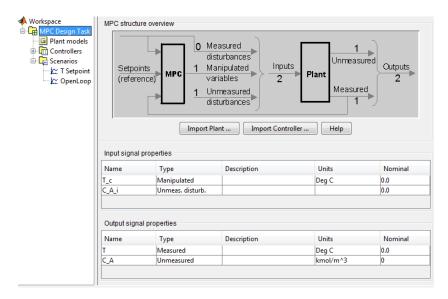


#### **Plant Model Importer Dialog Box**

The **Import from MATLAB workspace** option button should be selected by default, as shown. The **Items in your workspace** table lists your LTI models. If CSTR doesn't appear, define it as discussed in "State-Space Format" on page 2-5, then reopen this dialog box.

After CSTR appears, select it. The **Properties** list displays the number of inputs and outputs, their names and signal types, etc.

Click the **Import** button. This loads CSTR into the design tool. Then click the **Close** button (otherwise the dialog box remains visible in case you want to import another model). The design tool should appear as in Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5.



Model Predictive Control Toolbox Design Tool's Signal Definition View

#### **Signal Property Specifications**

The figure's graphical display indicates that you've imported a plant model by showing the number of inputs and outputs, and the number in each subclass: measured disturbance, manipulated variables, etc.). Also, the tables labeled **Input signal properties** and **Output signal properties** fill with data:

- The Name entries are from the CSTR model's InputName and OutputName properties (the design tool assigns defaults if necessary). You can edit these at any time.
- The **Type** entries are from the CSTR model's InputGroup and OutputGroup properties. (The design tool defaults all unspecified inputs to manipulated variables and all unspecified outputs to measured.)

**Note** Once you leave this view, if you subsequently change a signal type, you will have to restart the design. Be sure the signal types are correct at the beginning.

- The **Description** and **Unit** entries are optional. You can enter the values shown in Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5 manually. As you will see, the design tool uses them to label plots and other tables.
- The Nominal entries are initial conditions for simulations. The design tool default is 0.0.

# **Navigation Using the Tree View**

The *tree* in the left-hand frame of Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5 shows that the default **MPC Design Task** *node* (see Model Predictive Control Toolbox Design Tool Initial View on page 3-3) has been renamed **CSTRcontrol** by clicking the name, waiting for the usual edit box to appear, typing the new name, and pressing **Enter** to finalize the choice.

Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5 also shows three new nodes below **CSTRcontrol**. These activate once you've imported a plant model (or controller).

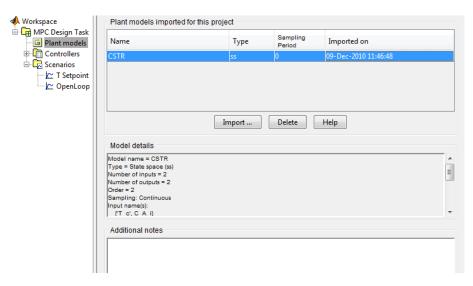
In general, clicking a node displays a *view* supporting a particular design activity.

#### **Project View (Signal Properties Tables)**

For example, clicking the *project* node (**CSTRcontrol** in Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5) allows you to review and edit the signal properties tables.

#### **Listing Your Plant Models**

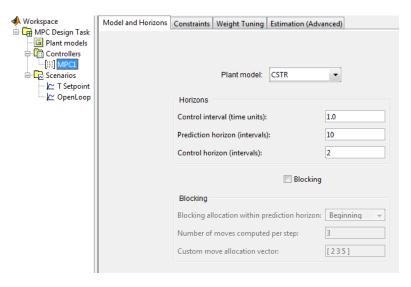
Select the **Plant models** node to list the plant models you've imported, as shown in Plant Models View with CSTR Model Selected on page 3-7. (Each model name is editable.) The **Model details** section displays properties of the selected model. There is also a space to enter notes describing the model's special features. Buttons allow you to import a new model or delete one you no longer need.



Plant Models View with CSTR Model Selected

#### **Viewing Your Controllers**

Next, select **Controllers**. The view shown in Controllers View on page 3-8 appears. A + sign to the left of **Controllers** indicates that it contains subnodes. You can click a + sign to expand the tree (as shown in Controllers View on page 3-8, where the + sign has changed to a – sign).



#### **Controllers View**

The table at the top of Controllers View on page 3-8 lists all the controllers you've defined. The design tool automatically creates a controller containing Model Predictive Control Toolbox defaults, naming it **MPC1**. It is a subnode of **Controllers**.

**Note** If you define additional controllers, they will appear here. For example, you might want to test several options, saving each as a separate controller, making it easy to switch from one to another during testing.

The table **Controllers defined in this project** allows you to edit the controller name and gives you quick access to three important design parameters: **Plant Model**, **Control Interval**, and **Prediction Horizon**. All are editable, but leave them at their default values for this example.

The buttons shown in Controllers View on page 3-8 let you do the following:

- Import a controller designed previously and stored either in your workspace or in a MAT-file.
- Export the selected controller to your workspace.

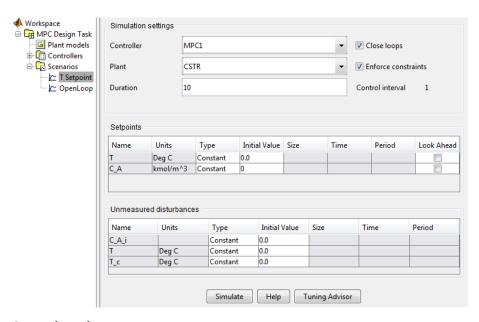
- Create a new controller initialized to Model Predictive Control Toolbox defaults.
- Copy the selected controller, creating a duplicate you can modify.
- Delete the selected controller.

You can also right-click the **Controllers** node to access menu options **New**, **Import**, and **Export**, or one of its subnodes to access menu options **Copy**, **Rename**, **Export**, and **Delete**.

Select the **MPC1** node to display Model Predictive Control Toolbox default controller settings. ("Changing Controller Settings" on page 3-19 covers this view in detail).

#### **Viewing Simulation Scenarios**

A *scenario* is a set of conditions defining a simulation. The design tool creates a default scenario and names it **Scenario1**. To view it, click the + symbol next to the **Scenarios** node, and select the **Scenario1** subnode. You should see a view like that shown in CSTR Temperature Setpoint Change Scenario on page 3-12.



#### **Scenarios View**

Whenever you select the Scenarios node, you see a table summarizing your current scenarios (not shown). Its function is similar to the Controllers view described previously.

#### **Linear Simulations**

You will usually want to test your controller in simulations. The Model Predictive Control Toolbox design tool makes it easy to run closed-loop simulations involving a Model Predictive Control Toolbox controller and an LTI plant model. This plant can differ from that used in the controller design, allowing you to test your controller's sensitivity to prediction errors (see "Robustness Testing" on page 3-43).

This section covers the following topics:

- "Defining Simulation Conditions" on page 3-11
- "Running a Simulation" on page 3-12
- "Open-Loop Simulations" on page 3-15

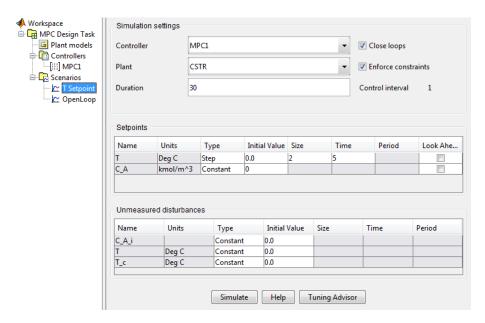
# **Defining Simulation Conditions**

To define simulation conditions, select an existing scenario node or create a new one, and then edit its tabular fields to define your conditions.

CSTR Temperature Setpoint Change Scenario on page 3-12 shows the result of renaming the default **Scenario1** node to **T Setpoint** and editing its default conditions. The required editing steps are as follows:

- Increase **Duration** from 10 to 30.
- Locate the tabular data defining the reactor temperature setpoint (first row of the upper table in CSTR Temperature Setpoint Change Scenario on page 3-12).
  - Click the Type table cell and select Step from the list of choices.
  - Change **Size** from 1.0 to 2.
  - Change **Time** from 1.0 to 5.

**Note** The **Control Interval** is a property of the controller being used (MPC1 in this case). To change it, select the controller node in the tree, and then edit the value on the **Model and Horizons** tab (see "Model and Horizons" on page 3-19). Such a change would apply to all simulations involving that controller.



**CSTR Temperature Setpoint Change Scenario** 

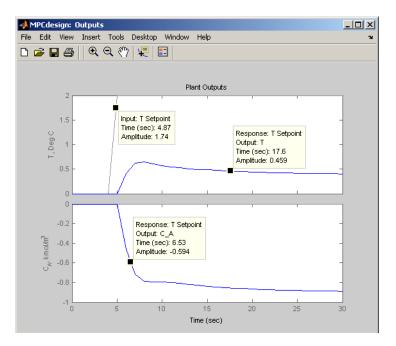
# **Running a Simulation**

To run a simulation, do *one* of the following:

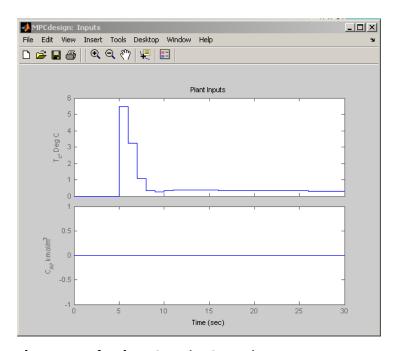
- Select the scenario you want to run, and click its **Simulate** button (see the bottom of CSTR Temperature Setpoint Change Scenario on page 3-12).
- Click the toolbar's **Simulation** button, which is the triangular icon shown on the top left of CSTR Temperature Setpoint Change Scenario on page 3-12.

The toolbar method runs the *current scenario*, i.e., the one most recently selected or modified.

Try running the **T Setpoint** scenario. This should generate the two response plot windows shown in Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 and Plant Inputs for the T Setpoint Scenario on page 3-14.



Plant Outputs for T Setpoint Scenario with Added Data Markers



#### Plant Inputs for the T Setpoint Scenario

Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 shows that the reactor temperature setpoint increases suddenly by 2 degrees at t=5, as you specified when defining the scenario in "Defining Simulation Conditions" on page 3-11. Unfortunately, the temperature does not track the setpoint very well, and there is a persistent error of about 1.6 degrees at the end of the simulation.

Also, the controller requests a sudden jump in the coolant temperature (see the upper graph in Plant Inputs for the T Setpoint Scenario on page 3-14), which might be difficult to deliver in practice. (The lower graph in Plant Inputs for the T Setpoint Scenario on page 3-14 shows that the feed concentration,  $C_{Ai}$ , remains constant, as specified in the scenario.)

See "Changing Controller Settings" on page 3-19 for ways to overcome these deficiencies.

**Note** Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 has *data markers*. To add these, left-click the curve to create the data marker. Drag a marker to relocate it. Left-click in a graph's white space to erase its markers. For more information on data markers, see the Control System Toolbox documentation.

# **Open-Loop Simulations**

By default, scenarios are *closed loop*, i.e., an active controller adjusts the manipulated variables entering your plant based on feedback from the plant outputs. You can also run *open-loop* simulations that test the plant model without feedback control.

For example, you might want to check your plant model's response to a particular input without opening another tool. You might also want to display unmeasured disturbance signals before using them in a closed-loop simulation.

To see how this works, create a new scenario by right-clicking the **T Setpoint** node in the tree, and selecting **Copy Scenario** in the resulting menu. Rename the copy **OpenLoop**.

Select **OpenLoop** in the tree. On its scenario view, change Duration to 100, and turn off (clear) **Close loops**.

Open-loop simulations ignore the **Setpoints** table settings, so there's no need to modify them.

If CSTR had a measured disturbance input, the pane would contain another table allowing you to specify it.

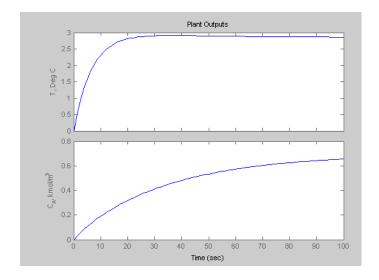
For this example, focus on the **Unmeasured disturbances** table. Configure it as shown below.

Unmeasured disturbances								
Name	Units	Туре	Initial Value	Size	Time	Period		
C_A_i	kmol/m^3	Constant	1					
T	Deg C	Constant	0.0					
T_c	Deg C	Constant	0.0					

The C\_A\_i input's nominal value is 0.0 (see Model Predictive Control Toolbox Design Tool's Signal Definition View on page 3-5), so the above models a sudden increase to 1 at the beginning of the simulation. The following is an equivalent setup using the Step type.

Unmeasured disturbances							
Name	Units	Туре	Initial Value	Size	Time	Period	
C_A_i	kmol/m^3	Step	0	1	0		
T	Deg C	Constant	0.0				
T_c	Deg C	Constant	0.0				

Using one of these, simulate the scenario (click its **Simulate** button). The output response plot should be as shown below.



This is the CSTR model's open-loop response to a unit step in the  ${\cal C}_{Ai}$  disturbance input.

You could also set up the table as shown below.

Unmeasured disturbances								
Name	Units	Туре	Initial Value	Size	Time	Period		
C_A_i	kmol/m^3	Constant	0.0					
T	Deg C	Constant	0.0					
T_c	Deg C	Constant	h					

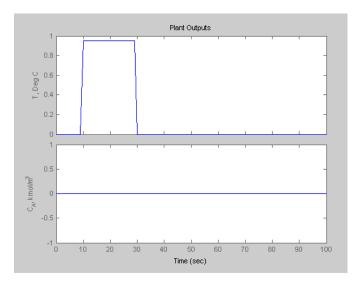
This simulation would display the open-loop response to a unit step in the  $T_c$  manipulated variable input (try it).

Finally, set it up as follows.

Unmeasured disturbances								
Name	Units	Туре	Initial Value	Size	Time	Period		
C_A_i	kmol/m^3	Constant	0.0					
T	Deg C	Pulse	0.0	0.95	10	20		
T_c	Deg C	Constant	0.0					

This adds a pulse to the T output. The pulse begins at time t = 10, and lasts 20 time units. Its height is 0.95 degrees.

Run the simulation. The output response plot displays the pulse (see Response Plot Showing Open-Loop Pulse Disturbance on page 3-17). In this case, the T output's nominal value is zero, so you only see the pulse. (If the T output had a nonzero nominal value, the pulse would add to that.)



#### **Response Plot Showing Open-Loop Pulse Disturbance**

If you were to run a *closed-loop* simulation with this same T disturbance, the controller would attempt to hold T at its setpoint, and the result would differ

from that shown in Response Plot Showing Open-Loop Pulse Disturbance on page 3-17.

# **Changing Controller Settings**

The simulations shown in Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 and Plant Inputs for the T Setpoint Scenario on page 3-14 used the default controller settings. These often work well, but the CSTR application is an exception. The following discussion covers the main controller options in more detail, and shows how to tune a controller for better performance.

This section covers the following topics:

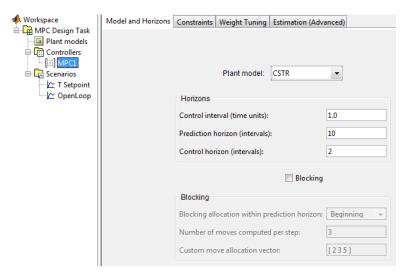
- "Model and Horizons" on page 3-19
- "Weight Tuning" on page 3-20
- "Blocking" on page 3-25
- "Defining Manipulated Variable Constraints" on page 3-29
- "Disturbance Modeling and Estimation" on page 3-31

#### Model and Horizons

Select your **MPC1** controller in the tree. The view shown in Controller Options — Model and Horizons Tab on page 3-20 should appear. If necessary, click the **Model and Horizons** tab to bring it to the front. This tab contains the following controller options:

- Plant model specifies the LTI model to be used for controller predictions.
- **Control interval** sets the elapsed time between successive adjustments of the controller's manipulated variables.
- Prediction horizon is the number of control intervals over which the outputs are to be optimized.
- **Control horizon** sets the number of control intervals over which the manipulated variables are to be optimized.
- Selecting the **Blocking** option gives you more control over the way in which the controller's *moves* are allocated.

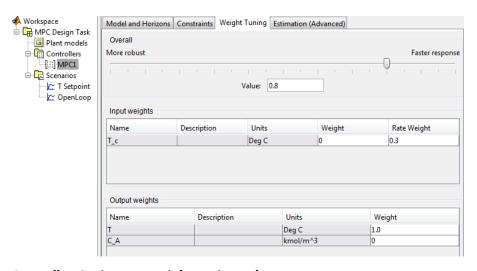
Leave all of the **Model and Horizons** tab settings at their default values for now.



Controller Options — Model and Horizons Tab

# **Weight Tuning**

Click the **Weight Tuning** tab. The view shown in Controller Options — Weight Tuning Tab on page 3-20 appears.



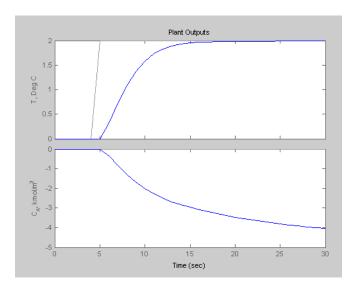
Controller Options — Weight Tuning Tab

Make the following changes (already done in the above view):

- In the **Input weights** section, change the coolant temperature's **Rate Weight** from the default 0.1 to 0.3.
- In the **Output weights** section, change the reactant concentration's **Weight** (last entry in the second row) from the default 1.0 to 0.

Test these changes using the **T Setpoint** scenario (click the toolbar's **Simulation** button).

Improved Setpoint Tracking for CSTR Temperature on page 3-21 shows that the CSTR temperature now tracks the setpoint change smoothly, reaching the new value in about 10 time units with no overshoot.



#### **Improved Setpoint Tracking for CSTR Temperature**

On the other hand, the reactant concentration,  $C_A$ , exhibits a larger deviation from its setpoint, which is being held constant at zero (compare to Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13, where the final deviation is about a factor of 4 smaller).

This behavior reflects an unavoidable trade-off. The controller has only one adjustment at its disposal: the coolant temperature. Therefore, it can't satisfy setpoints on both outputs.

#### **Output Weights**

The output weights let you dictate the accuracy with which each output must track its setpoint. Specifically, the controller predicts deviations for each output over the prediction horizon. It multiplies each deviation by the output's weight value, and then computes the weighted sum of squared deviations,  $S_{\nu}(k)$ , as follows

$$S_{y}(k) = \sum_{i=1}^{P} \sum_{j=1}^{n_{y}} \left\{ w^{y}_{j} [r_{j}(k+i) - y_{j}(k+i)] \right\}^{2}$$

where k is the current sampling interval, k+i is a future sampling interval (within the prediction horizon), P is the number of control intervals in the prediction horizon,  $n_y$  is the number of plant outputs,  $w^{y_j}$  is the weight for output j, and the term  $[r_j(k+i)-y_j(k+i)]$  is a predicted deviation for output j at interval k+1.

The weights must be zero or positive. If a particular weight is large, deviations for that output dominate  $S_y(k)$ . One of the controller's objectives is to *minimize*  $S_y(k)$ . Thus, a large weight on a particular output causes the controller to minimize deviations in that output (relative to outputs having smaller weights).

For example, the default values used to produce Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 specify equal weights on each output, so the controller is trying to eliminate deviations in both, which is impossible. On the other hand, the design of Improved Setpoint Tracking for CSTR Temperature on page 3-21 uses a weight of zero on the second output, so it is able to eliminate deviations in the first output.

**Note** The second output is unmeasured. Its predictions rely on the plant model and the temperature measurements. If the model were reliable, we could hold the predicted concentration at a setpoint, allowing deviations in the reactor temperature instead. In practice, it would be more common to control the temperature as done here, using the predicted reactant concentration as an auxiliary indicator.

You might expect equal output weights to result in equal output deviations at steady state. Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13 shows that this is not the case. The reason is that the controller is trying to satisfy several additional objectives simultaneously.

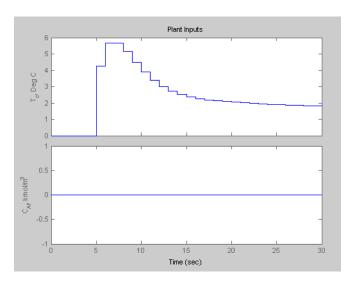
#### **Rate Weights**

One is to minimize the weighted sum of controller adjustments, calculated according to

$$S_{\Delta u}(k) = \sum_{i=1}^{M} \sum_{j=1}^{n_{mv}} \left\{ w_j^{\Delta u} \Delta u_j (k+i-1) \right\}^2$$

where M is the number of intervals in the control horizon,  $n_{mv}$  is the number of manipulated variables,  $\Delta u_j(k+i-1)$  is the predicted adjustment in manipulated variable j at future (or current) sampling interval k+i-1,

and  $w_j^{\Delta u}$  is the weight on this adjustment, called the *rate weight* because it penalizes the incremental change rather than the cumulative value. Increasing this weight forces the controller to make smaller, more cautious adjustments.



#### **Plant Inputs for Modified Rate Weight**

Plant Inputs for Modified Rate Weight on page 3-24 shows that increasing the rate weight from 0.1 to 0.3 decreases the move sizes significantly, especially the initial move (compare to Plant Inputs for the T Setpoint Scenario on page 3-14).

Setting the rate weight to 0.1 yields a faster approach to the T setpoint with a small overshoot, but the initial  $T_c$  move is about six times larger than needed to achieve the new steady state, which would be unacceptable in most applications (not shown; try it).

**Note** The controller minimizes the sum  $S_y(k) + S_{\Delta u}(k)$ . Changes in the coolant temperature have unequal effects on the two outputs, so the steady-state output deviations won't be equal, even when both output weights are unity as in Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13.

#### **Input Weights**

The controller also minimizes the weighted sum of manipulated variable deviations from their nominal values, computed according to

$$S_{u}(k) = \sum_{i=1}^{M} \sum_{j=1}^{n_{mv}} \left\{ w_{j}^{u} [u_{j}(k+i-1) - \overline{u}_{j}] \right\}^{2}$$

where  $w_j^u$  is the *input weight* and  $\bar{u}_j$  is the nominal value for input j. In the above simulations, you used the default,  $w_j^u = 0$ . This is the usual choice.

When a sustained disturbance or setpoint change occurs, the manipulated variable must deviate permanently from its nominal value (as shown in Plant Inputs for the T Setpoint Scenario on page 3-14 and Plant Inputs for Modified Rate Weight on page 3-24). Using a nonzero input weight forces the corresponding input back toward its nominal value. Test this by running a simulation in which you set the input weight to 1. The final  $T_c$  value is closer to its nominal value, but this causes T to deviate from the new setpoint (not shown).

**Note** Some applications involve more manipulated variables than plant outputs. In such cases, it is common to define nonzero input weights on certain manipulated variables in order to hold them near their most economical values. The remaining manipulated variables eliminate steady-state error in the plant outputs.

## **Blocking**

The section "Weight Tuning" on page 3-20 used *penalty weights* to shape the controller's response. This section covers the following topics:

- An alternative to penalty weighting, called *blocking*
- Side-by-side controller comparisons

To begin, select **Controllers** in the tree, and click the **New** button, creating a controller initialized to the Model Predictive Control Toolbox default settings. Rename this controller **Blocking 1** by editing the appropriate table cell.

Select **Blocking 1** in the tree, select its **Weight Tuning** tab, and set the **Weight** for output C\_A to 0 (see "Weight Tuning" on page 3-20 to review the reason for this). Leave other weights at their defaults.

Now select the **Model and Horizons** tab, and select its **Blocking** check box. This activates the blocking options. It also deactivates the **Control Horizon** option (the blocking options override it).

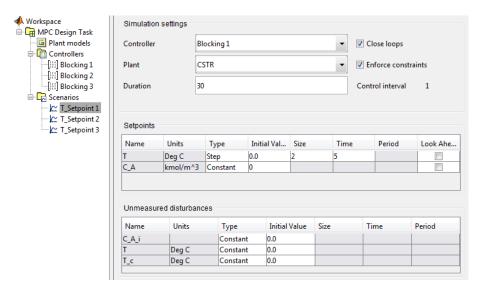
Set Number of moves computed per step to 2. Verify that Blocking allocation within prediction horizon is set to Beginning, the default.

Select **Controllers** in the tree, and use its **Copy** button to create two controllers based on **Blocking 1**. Rename these **Blocking 2** and **Blocking 3**. Edit their blocking options, setting **Blocking allocation within prediction** horizon to Uniform for **Blocking 2**, and to End for **Blocking 3**.

Select **Scenarios** in the tree. Rename the **T Setpoint** scenario to **T Setpoint** 1, and set its **Controller** option to **Blocking** 1.

Create two copies of **T Setpoint 1**, naming them **T Setpoint 2** and **T Setpoint 3**. Set their **Controller** options to **Blocking 2** and **Blocking 3**, respectively. Now you should have three scenarios, identical except for the controller being used.

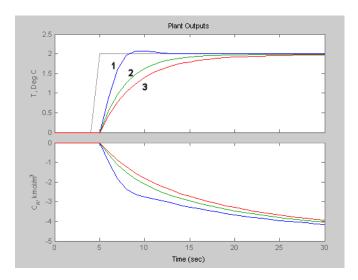
Delete the **MPC1** controller and select **T Setpoint 1** in the tree. Your view should resemble T Setpoint 1 Scenario on page 3-27, with three controllers and three scenarios in the tree.



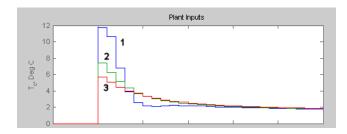
#### T Setpoint 1 Scenario

If any simulation plot windows are open, close them. This forces subsequent simulations to generate new plots.

Simulate each of the three scenarios. When you run the first, new plot windows open. Leave them open when you run the other two scenarios so all three results appear together, as shown in Blocking Comparison, Outputs on page 3-28 and Blocking Comparison, Manipulated Variable on page 3-28.



#### **Blocking Comparison, Outputs**



#### **Blocking Comparison, Manipulated Variable**

The numeric annotations on these figures refer to the three scenarios. Recall that **T Setpoint 1** uses the default blocking, which usually results in faster setpoint tracking but larger manipulated variable moves. The blocking options in **T Setpoint 2** and **T Setpoint 3** reduce the move size but make setpoint tracking more sluggish.

Results for **T Setpoint 3** are very similar to those shown in Improved Setpoint Tracking for CSTR Temperature on page 3-21 and Plant Inputs for Modified Rate Weight on page 3-24, where a penalty *rate weight* reduced the move sizes. If rate weights and blocking achieve the same ends, why does the toolbox provide both features? One difference not evident in this simple

problem is that blocking applies to all the manipulated variables in your application, but each rate weight affects one only.

**Note** To obtain the dashed lines shown for **T Setpoint 2**, activate the plot window and select **Property Editor** from the **View** menu. The Property Editor appears at the bottom of the window. Then select the curve you want to edit. The Property Editor lets you change the line type, thickness, color, and symbol type. Select the axis labels to see additional options.

By default, the toolbox plots each scenario on the same plot. If you recalculate a revised scenario, it replots that result but doesn't change any others.

If you don't want to see a particular scenario, right-click the plot and use the **Responses** menu option to hide it. (You can also close the plot window and recalculate selected responses in a fresh window.)

## **Defining Manipulated Variable Constraints**

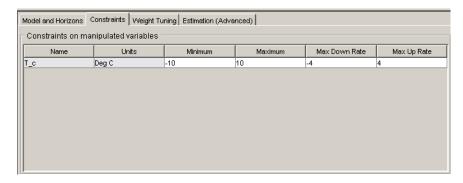
Physical devices have limited ranges and rates of change. For example, the CSTR model's coolant might be restricted to a 20 degree range (from -10 to 10) and its maximum rate of change might be  $\pm 4$  degrees per control interval. If these are true physical restrictions, it's good practice to include them in the controller design. Otherwise the controller might attempt an unrealistic adjustment.

To compare constrained and unconstrained performance for the CSTR example, select the **Blocking 1** controller in the tree, and rename it **Unconstrained**.

Select its **Model and Horizons** tab and turn off (clear) its **Blocking** option. Increase **Control horizon** to 3, and reduce **Control Interval** to 0.25.

Delete the **Blocking 2** and **Blocking 3** controllers. (Click **Yes** or **OK** to dismiss the resulting warning messages.)

Copy the **Unconstrained** controller. Name this copy **MVconstraints**, and select its **Constraints** tab. Then enter the manipulated variable constraints shown in Entering CSTR Manipulated Variable Constraints on page 3-30.



### **Entering CSTR Manipulated Variable Constraints**

If any simulation plot windows are open, close them (to force fresh plots).

Select the **T Setpoint 1** scenario. If necessary, set its **Controller** option to Unconstrained. Change **Duration** to 15, and simulate the scenario.

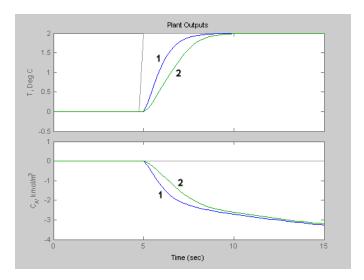
Select the **T Setpoint 2** scenario, set its **Controller** option to MVconstraints, change its **Duration** to 15, and simulate it. The results appear in CSTR Outputs, Unconstrained (1) and MVconstraints (2) on page 3-31 and CSTR Manipulated Variable, Unconstrained (1) and MVconstraints (2) on page 3-31.

The larger control horizon and smaller control interval cause the unconstrained controller to make larger moves (see CSTR Manipulated Variable, Unconstrained (1) and MVconstraints (2) on page 3-31, curve 1). The output settles at the new setpoint in about 5 time units rather than the 10 required previously (compare curve 1 in CSTR Outputs, Unconstrained (1) and MVconstraints (2) on page 3-31 to curve 1 in Blocking Comparison, Outputs on page 3-28).

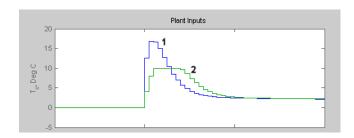
CSTR Manipulated Variable, Unconstrained (1) and MVconstraints (2) on page 3-31 (curve 2) shows that the **Max Up Rate** constraint limits the size of the first two moves to 4 degrees. The third move hits the **Maximum** constraint at 10 degrees. The coolant temperature remains saturated at its upper limit for the next 7 control intervals, then slowly moves back down to its final value.

CSTR Outputs, Unconstrained (1) and MVconstraints (2) on page 3-31 (curve 2) shows that the output response is slower, but still settles at the

new setpoint smoothly within about 5 time units. This demonstrates the *anti-windup* protection provided automatically by the Model Predictive Control Toolbox controller.



CSTR Outputs, Unconstrained (1) and MVconstraints (2)



CSTR Manipulated Variable, Unconstrained (1) and MVconstraints (2)

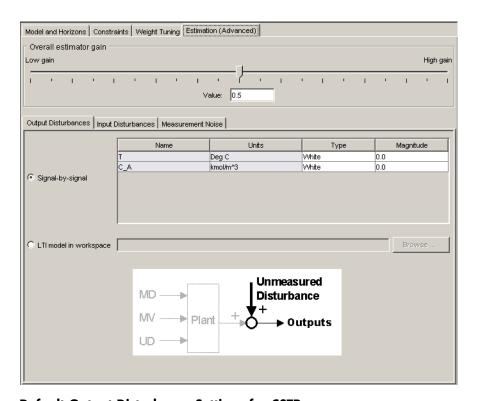
## **Disturbance Modeling and Estimation**

The previous sections tested the controller's response to setpoint changes. In process control, disturbances rejection is often more important. The Model Predictive Control Toolbox product allows you to tailor the controller's disturbance response. The following example assumes that you have just completed the previous section, and the design tool is still open.

Select the first controller in the tree and rename it **InputSteps**. (Its settings should be identical to the **Unconstrained** controller of the previous section.)

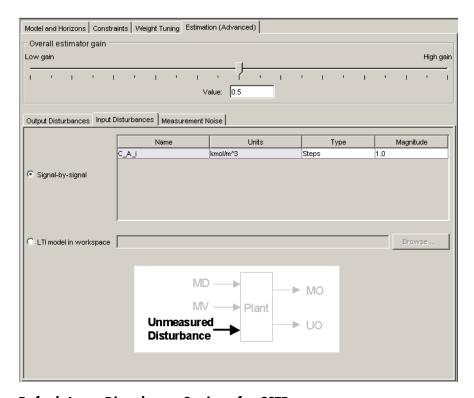
Copy this controller. Rename the copy **OutputSteps**. Click its **Estimation** tab. The initial view should be as in Default Output Disturbance Settings for CSTR on page 3-33. Note the following:

- Model Predictive Control Toolbox default settings are being used. (The **Use Model Predictive Control Defaults** button restores these settings if you modify them.)
- The **Output Disturbances** tab is selected, and the **Signal-by-signal** option is selected. The graphic shows that the output disturbances add to each output.
- The tabular entries show, however, that these disturbance magnitudes are currently zero.



**Default Output Disturbance Settings for CSTR** 

Click the **Input Disturbances** tab. (This would be inactive if the plant model had no unmeasured disturbances.) The view should change to that shown in Default Input Disturbance Settings for CSTR on page 3-34.



#### **Default Input Disturbance Settings for CSTR**

In this case the disturbance magnitude is nonzero, and the disturbance type is Steps. Thus, the controller assumes that disturbances enter as random steps (integrated white noise) at the plant's unmeasured disturbance input.

Click the **Measurement Noise** tab, verifying that the controller is assuming white noise, magnitude 1 (not shown).

The following summarizes Model Predictive Control Toolbox default disturbance modeling assumptions for this case:

- Additive output disturbances: none
- Unmeasured input disturbances: random steps (integrated white noise)
- Measurement noise: white

In general, if your plant model includes unmeasured disturbance inputs, the toolbox default strategy will assume that they are dominant and sustained, as in the above example. This forces the controller to include an integrating mode, intended to eliminate steady-state error.

If the plant model contains no unmeasured input disturbances, the toolbox assumes sustained (integrated white noise) disturbances at the measured plant outputs.

If there are more measured outputs than unmeasured input disturbances, it assumes sustained disturbances in both locations according to an algorithm described in the product's online documentation.

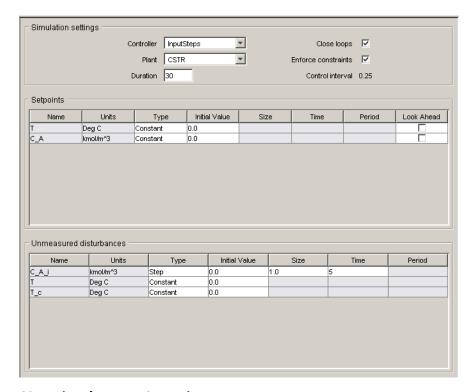
In any case, the design tool displays the assumptions being used.

To modify the estimation strategy in the OutputSteps controller, do the following:

- Click the **Input Disturbances** tab. Set the disturbance **Type** to White, and its **Magnitude** to 0.
- Click the **Output Disturbances** tab. For the T output, set the disturbance Type to Steps, and its magnitude to 1.

This *reverses* the default assumptions, i.e., the **OutputSteps** controller assumes that sustained disturbances enter at the plant output rather than at the unmeasured disturbance input. The **InputSteps** controller is still using the original (default) assumptions.

Next, select the first scenario in the tree. Rename it **Disturbance 1**, set its **Duration** to 30, define all setpoints as constant zero values, and define a unit-step disturbance in the unmeasured input, C\_A\_i. If necessary, set its **Controller** option to InputSteps . CSTR Disturbance 1 Scenario on page 3-36 shows the final **Disturbance 1** scenario.



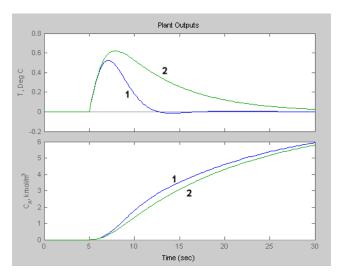
#### **CSTR Disturbance 1 Scenario**

Copy **Disturbance 1**. Rename the copy **Disturbance 2**, and set its **Controller** option to OutputSteps.

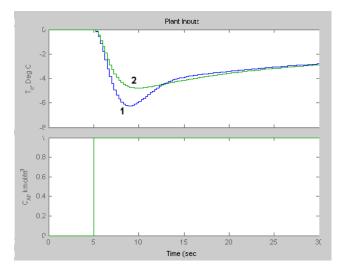
If necessary, close any open simulation plot windows. Simulate both scenarios. CSTR Outputs for Disturbance Scenarios 1 and 2 on page 3-37 and CSTR Inputs for Disturbance Scenarios 1 and 2 on page 3-37 show the results.

CSTR Outputs for Disturbance Scenarios 1 and 2 on page 3-37 shows that default controller (case 1) returns to the setpoint in less than one third the time required by the modified controller (case 2). Its maximum deviation from the setpoint is also 10% smaller. CSTR Inputs for Disturbance Scenarios 1 and 2 on page 3-37 shows that in both cases the input moves are smooth and of reasonable magnitude. (It also shows the input disturbance.)

The default controller expects unmeasured disturbances to enter as defined in the scenarios, so it's not surprising that the default controller performs better. The point is that the difference can be large, so it merits design consideration.

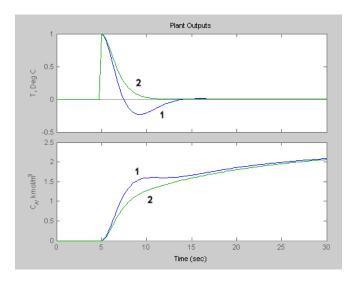


CSTR Outputs for Disturbance Scenarios 1 and 2



CSTR Inputs for Disturbance Scenarios 1 and 2

For comparison, reset the two scenarios so that the only disturbance is a one-degree step increase added to the measured reactor temperature. The modified controller (case 2) is designed for such disturbances, and CSTR Outputs, Output Disturbance Scenarios 1 and 2 on page 3-38 shows that it performs better, but the difference is less dramatic than in the previous scenario. The default controller is likely to be best if the real process has multiple dominant disturbance sources.



CSTR Outputs, Output Disturbance Scenarios 1 and 2

# **Defining Soft Output Constraints**

The discussion in "Weight Tuning" on page 3-20, defined temperature control as the primary goal for the CSTR application. The predicted (but unmeasured) reactant concentration,  $C_4$ , could vary freely.

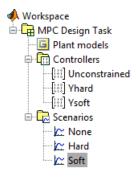
Suppose this were acceptable provided that  $C_A$  stayed below a specified maximum (above which unwanted reactions would occur). You can use an *output constraint* to enforce this specification.

Start with a single controller identical to the **InputSteps** controller described in "Disturbance Modeling and Estimation" on page 3-31. Rename it **Unconstrained**.

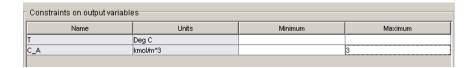
Right-click **Unconstrained** in the tree and select **Copy**. Rename the copy **Yhard**. Make another copy, naming it **Ysoft**.

Similarly, start with a single scenario identical to CSTR Disturbance 1 Scenario on page 3-36, except that its **Controller** setting should be Unconstrained. Name this scenario **None**.

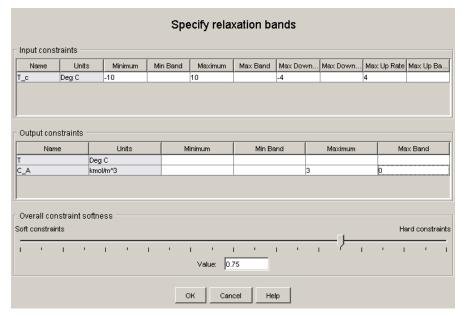
Right-click **None** in the tree and select **Copy**. Rename the copy **Hard**, and change its **Controller** setting to Yhard. Make another copy, naming it **Soft** and changing its **Controller** setting to Ysoft. Your tree should be as shown below.



Select your **Yhard** controller. On the **Constraints** tab, set the maximum for  $C_A$  to 3 as shown below.



Click the **Constraint Softening** button to open the dialog box in Constraint Softening Dialog Box on page 3-40. The **Input constraints** section shows the bounds on the inputs and their rates, and *relaxation bands*, which let you *soften* these constraints. By default, input constraints are *hard*, meaning that the controller tries to prevent any violation.

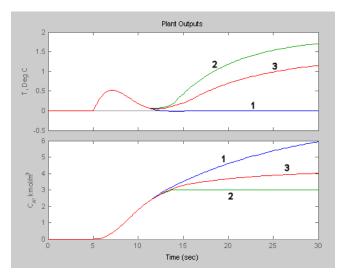


### **Constraint Softening Dialog Box**

The **Output constraints** section lists the output limits and their relaxation bands. By default, the output constraints are *soft*. Make the  $C_A$  upper limit hard by entering a zero as its relaxation band (as in Constraint Softening Dialog Box on page 3-40).

Select the **Ysoft** controller. Define a soft upper bound on  $C_A$  by using the same settings shown in Constraint Softening Dialog Box on page 3-40, but with a relaxation band of 100 instead of 0.

Simulate the three scenarios in the order they appear in the tree, i.e., **None**, **Hard**, **Soft**. The resulting output responses appear in Constraint Softening Scenarios: 1 = None, 2 = Hard, 3 = Soft on page 3-41.



Constraint Softening Scenarios: 1 = None, 2 = Hard, 3 = Soft

Curve 1 is without output constraints, which is identical to curve 1 in CSTR Outputs for Disturbance Scenarios 1 and 2 on page 3-37. This controller allows the  $C_A$  output to vary freely, but the controlled temperature returns to its setpoint within 10 time units after the disturbance happens.

Curve 2 shows the behavior with a hard upper limit at  $C_A$  = 3. Once  $C_A$  reaches this bound, the controller must use its one manipulated variable ( $T_c$ ) to satisfy the constraint, so it's no longer able to control the temperature.

Curve 3 shows the result for a soft constraint. The controller reaches a compromise between the competing objectives: temperature control and constraint satisfaction. As you'd expect, performance lies between the curve 1 and curve 2 extremes.

The numerical value of the relaxation band represents a *relative tolerance* for constraint violations, not a strict limit (if it were the latter, it would be a hard constraint). If you were to increase its relaxation band (currently set at 100), performance would move toward Case 1, and vice versa.

If you have multiple constraints, you can harden or soften them simultaneously using the slider at the bottom of the controller's constraint softening dialog box (see Constraint Softening Dialog Box on page 3-40).

In general, you'll have to experiment to determine the settings that provide appropriate trade-offs for your application. In particular, the relaxation band settings interact with those on the controller's **Weight Tuning** tab (see "Weight Tuning" on page 3-20).

Another important factor is the expected numerical range for each variable. For example, if a particular variable stays within  $\pm 0.1$  of its nominal value, it should have a small relaxation band relative to another variable having a range of  $\pm 100$ .

For details on the Model Predictive Control Toolbox constraint softening formulation, see "Optimization Problem" in the *Model Predictive Control Toolbox User's Guide*.

# **Robustness Testing**

It's good practice to test your controller's sensitivity to prediction errors. Classical phase and gain margins are one way to quantify robustness for a SISO application. Robust Control Toolbox<sup>TM</sup> software provides sophisticated approaches for MIMO systems. It can also be helpful to run simulations. The following example illustrates the simulation approach.

### **Plant Model Perturbation**

Use the following code to create a perturbed version of the CSTR model:

```
CSTRp = CSTR;

CSTRp.a=[-0.0303 -0.0113 -0.0569 -0.1836];

CSTRp.b=[-0.0857 0.0191 0.1393 0.4241];
```

This creates a copy of CSTR called CSTRp, then replaces the state space A and B matrices with perturbed versions (compare to the originals defined in "State-Space Format" on page 2-5). Use the following command to compare the two step responses:

```
step(CSTR, CSTRp)
```

Observe the difference in the responses (not shown).

Select **Plant models** in the tree. Click the **Import** button and import the CSTRp model.

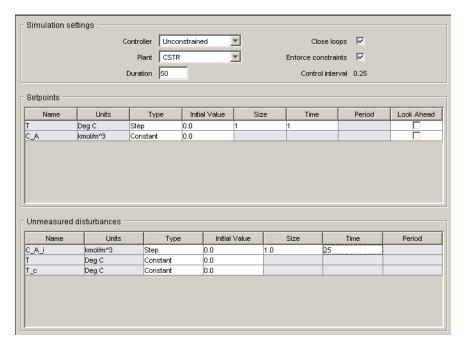
### **Simulation Tests**

Delete all controllers except the first one in the tree. If necessary, make its settings identical to **Unconstrained** (see "Defining Manipulated Variable Constraints" on page 3-29).

Delete all scenarios except the first, naming that **Accurate Model**. Define its properties as shown in Robustness Test, Accurate Plant Model Scenario on page 3-44. The scenario begins with a step change in the temperature

setpoint, followed 25 time units later by a step disturbance in the reactant entering the CSTR.

Copy **Accurate Model**. Rename the copy **Perturbed Model**, and set its **Plant** option to CSTRp. Thus, both scenarios use the same controller, which is based on the CSTR model, but the **Perturbed Model** scenario uses a different model to represent the "real" plant. This tests the controller's robustness to a change in plant parameters.

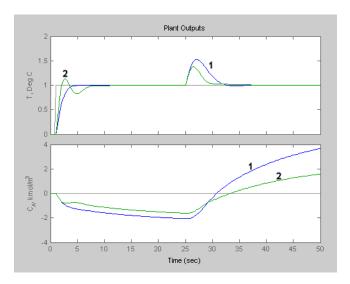


#### Robustness Test, Accurate Plant Model Scenario

Simulate the two scenarios. Robustness Test, Accurate Model (1) and Perturbed Model (2) on page 3-45 shows the output responses. As expected, setpoint tracking degrades when the model is inaccurate, but performance is still acceptable.

The disturbance rejection appears to *improve* with the perturbed model. This is a consequence of the perturbations used. The gain for the  $T/C_{Ai}$  output/input pair is about 15% smaller in the CSTRp model, which has two

beneficial effects: the actual impact of the disturbance is reduced, and the controller is aggressive because it expects a larger impact.



Robustness Test, Accurate Model (1) and Perturbed Model (2)

**Note** MIMO applications are usually more sensitive to model error than SISO applications, so robustness testing is especially recommended for MIMO cases.

# Plant Models with Delays

Unlike many controller design approaches, the Model Predictive Control Toolbox can handle models that include delays. A typical example is the distillation column model, DC, introduced in "Multiinput-Multioutput (MIMO) Plants" on page 2-11. The model includes a delay in each input/output channel.

The presence of delays will influence controller performance, and your controller specifications should account for them. The following example provides some guidelines and covers the following topics:

- "Importing the Plant Model" on page 3-46
- "Specifying Controller Horizons" on page 3-47

## Importing the Plant Model

To learn how to create the DC model, see "Multiinput-Multioutput (MIMO) Plants" on page 2-11. You must import the DC model into the MATLAB workspace.

Start the Model Predictive Control Toolbox design tool (type mpctool at the MATLAB command line). Import the DC model (see "Loading a Plant Model" on page 3-3).

Select **Plant models** in the tree. The DC model should be the only one listed. Scroll the **Model details** view to show the last few lines, which should appear as in DC Model Details, Maximum Delay Values on page 3-46.

```
Model details

Input group(s):

MV: [1 2]

MD: [3]

Output name(s):

{ Distillate Purity', 'Bottoms Purity'}

Output group(s):

MD: [1 2]

Maximum input delay: 4.000000e-001

Maximum output delay: 3

Maximum i/o delay: 6.700000e+000
```

DC Model Details, Maximum Delay Values

## **Specifying Controller Horizons**

The model's maximum I/O delay is 6.7 minutes. It is good practice to specify the prediction and control horizons such that

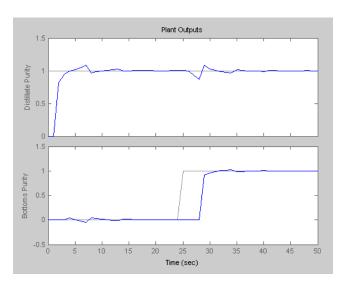
$$P - M \square t_{d.max} / \Delta t$$

where P is the prediction horizon, M is the control horizon,  $t_{d,max}$  is the maximum delay, and  $\Delta t$  is the control interval.

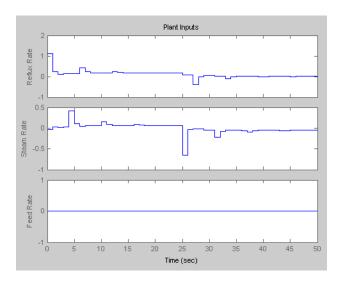
Select MPC1 (the default controller name) in the tree. Click the Model and Horizons tab, and set Control interval to 1, a reasonable choice if the closed-loop response time is to be of order 5-10 minutes.

Given the amount of plant delay and the specified control interval, the default horizons, P = 10, M = 2, would be a poor choice. Instead, set **Prediction** horizon to 30, and **Control horizon** to 5.

Select **Scenario1** in the tree. Set **Duration** to 50. Define a constant setpoint of 1 for the first output (the distillate purity). Define a step increase of 1 in the second output's setpoint, occurring at t = 25. All other signals should be zero. Simulate the scenario. DC Setpoint Response Scenario, Outputs on page 3-48 and DC Setpoint Response Scenario, Inputs on page 3-48 show the results.



### DC Setpoint Response Scenario, Outputs



### DC Setpoint Response Scenario, Inputs

As seen in DC Setpoint Response Scenario, Outputs on page 3-48, the first output cannot respond for a minimum of one minute, the delay in the  $y_1/u_1$  transfer function. After that, it reaches the setpoint in two minutes and

settles quickly. Similarly,  $y_2$  cannot respond for a minimum of three minutes, the delay in the  $y_2/u_2$  transfer function, but settles rapidly thereafter. Changing one setpoint disturbs the other output, but the magnitude of this *interaction* is less than 10%.

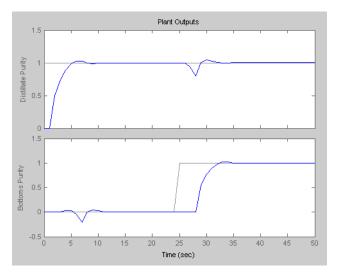
DC Setpoint Response Scenario, Inputs on page 3-48 shows that the initial input moves are more than five times the final change. Also, there are periodic pulses in the control action as the controller attempts to counteract the delayed effects of each input on the two outputs.

You can moderate these effects using the weights (see "Weight Tuning" on page 3-20). Instead, define a custom blocking strategy as illustrated in DC Model, Custom Blocking Strategy on page 3-49. This uses five moves as before, but allocates them more uniformly over the prediction horizon.

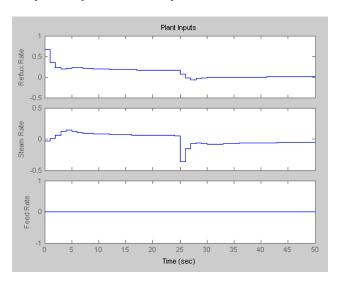
Output Responses for Setpoint Scenario with Blocking on page 3-50 and Input Moves for Setpoint Scenario with Blocking on page 3-50 show the corresponding simulation results. The initial input moves are much smaller, and the moves are less oscillatory overall. The trade-off is a slower output response with about 20% interaction.

Model and Horizons   Constraints	Weight Tuning   Estimation (Advanced)	
	Plant model: DC	▼
		_
[ ·	Horizons	
С	Control interval (time units):	1.0
P	rediction horizon (intervals):	30
c	Control horizon (intervals):	5
	<b>☑</b> Blocking	
r €	Blocking	
В	Blocking allocation within prediction horizon:	Custom
N	lumber of moves computed per step:	5
c	Custom move allocation vector:	555510]

DC Model, Custom Blocking Strategy



**Output Responses for Setpoint Scenario with Blocking** 



Input Moves for Setpoint Scenario with Blocking

# **Nonsquare Plants**

A *nonsquare* plant has an unequal number of manipulated variables and output variables. This is common in practice, and the Model Predictive Control Toolbox software supports an excess of manipulated variables or outputs. In such cases you will usually need to modify default toolbox settings.

This section covers the following topics:

- "More Outputs Than Manipulated Variables" on page 3-51
- "More Manipulated Variables Than Outputs" on page 3-52

## **More Outputs Than Manipulated Variables**

When there are excess outputs, you can't hold each at a setpoint. You have the following options:

- **1** Enforce setpoints on all outputs, in which case all will deviate from their setpoints to some extent.
- **2** Specify that certain outputs need not be held at setpoints by setting their weights to zero on the controller's **Weight Tuning** tab.

The initial test of the CSTR controller used option 1 (the default), which caused both outputs to deviate from their setpoints (see Plant Outputs for T Setpoint Scenario with Added Data Markers on page 3-13). You can adjust the offset in each output by changing the output weights. Increasing an output weight decreases the offset in that output (at the expense of increased offset in other outputs).

The modified CSTR controller used option 2 (see the discussion in "Weight Tuning" on page 3-20). In general, if the application has  $N_e$  more outputs than manipulated variables, setting  $N_e$  output weights to zero should allow the remaining outputs to be held at setpoints (unless the manipulated variables are constrained). This was the case for the modified CSTR controller (see Improved Setpoint Tracking for CSTR Temperature on page 3-21).

Outputs that have been "sacrificed" by setting their weights to zero can still be useful. If measured, they can help the controller to estimate the plant's state,

thereby improving its predictions. They can also be used as indicators, or as variables to be held within an operating region defined by output constraints.

## **More Manipulated Variables Than Outputs**

In this situation, default Model Predictive Control Toolbox settings should provide offset-free output-setpoint tracking, but the manipulated variables are likely to drift.

One way to avoid this is to use  $manipulated\ variable\ set points$ . If there are  $N_e$  excess manipulated variables and you hold  $N_e$  of them at target values, the rest should not drift. Rather, they will attain the values needed to eliminate output offset.

To define a manipulated variable setpoint:

- Enter the setpoint value in the Nominal field in the signal properties view

   see Model Predictive Control Toolbox Design Tool's Signal Definition
   View on page 3-5.
- 2 Assign a nonzero *input weight* using the **Weight** entry on the controller's **Weight Tuning** tab see Controller Options Weight Tuning Tab on page 3-20.

In step 2, the magnitude of the input weight determines the extent to which the manipulated variable can deviate from its target during a transient. See "Input Weights" on page 3-24 for more discussion and mathematical details.

You might want to allow such deviations temporarily in order to provide better output setpoint tracking. In that case, use a relatively small input weight. If you want the manipulated variable to stay near its target value at all times, increase its input weight.

Another way to avoid drift is to constrain one or more manipulated variables to a narrow operating region. You can even hold an MV constant by setting its lower and upper bounds to the same value (in which case its nominal value should also be set to this value), or by setting both of its rate constraints to zero. To define constraints, use the controller's **Constraints** tab (see "Defining Manipulated Variable Constraints" on page 3-29).

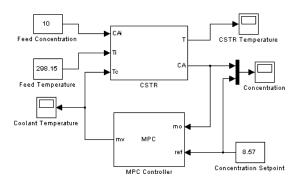
## **Nonlinear Plants**

You can control a Simulink plant modeled using a Model Predictive Control Toolbox Simulink block. This section illustrates the procedure using the nonlinear CSTR model introduced earlier (see "Using Simulink® Control Design™ to Linearize Simulink Model" on page 2-14). It covers the following topics:

- "MPC Controller Block" on page 3-53
- "Initiating the Controller Design" on page 3-54
- "Validating the Linearized Model" on page 3-57
- "Modifying the Linearized Model" on page 3-59
- "Linear Simulation Tests" on page 3-60
- "Nonlinear Simulation Tests" on page 3-61
- "Modifying the Controller Using the Design Tool" on page 3-64
- "Exiting the Design Tool" on page 3-64

### **MPC Controller Block**

Simulink Model for CSTR Control on page 3-54 shows CSTR with an added MPC Controller block. (The model is called CSTR\_MPC.mdl in the Model Predictive Control Toolbox demos folder.) The intent is to hold the residual concentration at a setpoint by adjusting the coolant temperature. The feed concentration and temperature inputs are disturbances, and the reactor temperature is an auxiliary, uncontrolled output. The concentration has a setpoint (reference), currently fixed at 8.57.

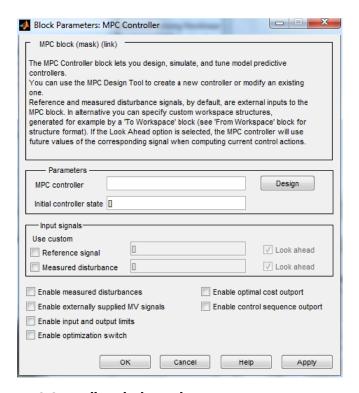


**Simulink Model for CSTR Control** 

**Note** If you have Model Predictive Control Toolbox software and Simulink installed, the MPC Controller block appears in your Simulink block library. If necessary, see the Simulink documentation for details on how to use library blocks to construct a model.

## **Initiating the Controller Design**

Once you've installed an MPC Controller block in your Simulink model, as in Simulink Model for CSTR Control on page 3-54, you need to configure it. Click it to open its *block mask*, and verify that it is as shown below.

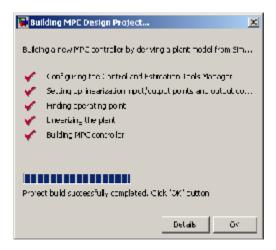


#### **MPC Controller Block Mask**

If you had used the design tool to create a controller and had saved it in your workspace, you could type its name in the **MPC controller** box and you'd be ready to test it.

Instead, create the controller using the Model Predictive Control Toolbox design tool. To do so, click the **Design** button. A dialog box (not shown) asks you to enter the number of *manipulated variables*, which are the plant inputs the controller can adjust to achieve its objectives. The coolant temperature is the only manipulated variable. Verify that the dialog box entry is 1 and click **OK**.

The following progress window marks the completion of each controller initialization step.



#### They are as follows:

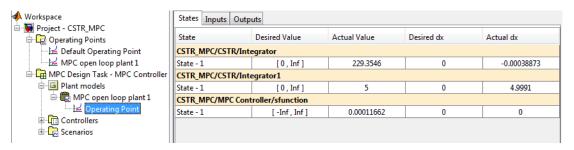
- 1 Open the Control and Estimation Tools Manager, and install a *project* having the same name as the Simulink model (CSTR MPC in this case).
- **2** Install a *linearization task* within the project and determine the plant's I/O points, i.e., the signals connected to the MPC Controller block's mv (manipulated variable) and mo (measured output) ports.
- **3** Determine a default *operating point*. This requires assumptions that might be incorrect, as demonstrated in the next section. In particular, the default outputs are zero.
- **4** Calculate a *linearized plant model* at this operating point using the linearization tool in Simulink® Control Design (see "Linearization Using Linear Analysis Tool in Simulink Control Design" on page 2-17). The controller is open loop during this step and involves only the blocks between the plant inputs and outputs (as determined in step 2).
- 5 Install a Model Predictive Control Toolbox design task in the project. Use the linearized model from step 4 to define a default controller (named MPC1), and enter its name as the block mask's MPC controller parameter.

When the last step has been completed, click **OK** to close the progress window.

## Validating the Linearized Model

Automatic linearization requires assumptions that might be incorrect. You should always validate a linearized model before using it in a controller.

As shown below, the controller task is the **MPC Controller** node, the name of the corresponding Simulink block.



**Note** In general, a Simulink model can contain multiple controllers, in which case the project would include multiple controller design tasks, each with a unique name.

Start by examining the default operating point. Expand the tree until it appears as above, and then select **Operating Point**. The **States** tab should be active as shown (if not, click it).

By default, the Simulink Control Design linearization tool tries to find a steady-state point, i.e., it sets the **Desired dx** column to zero. As shown above, the **Actual dx** column contains one value that is far from zero (4.9991), i.e., it has failed to achieve this goal.

**Note** Don't be concerned if you see numerical values that differ slightly from those shown.

Next, click the **Outputs** tab. By default, the linearization tool sets the desired plant output to zero. In the CSTR, this would require 100% conversion of the

reactant, which is impossible, and the **Outputs** tab confirms that the desired values were not achieved.

Finally, export the linearized model to your workspace. Right-click the **MPC open loop plant 1** node and choose **Export** to open the following dialog box.

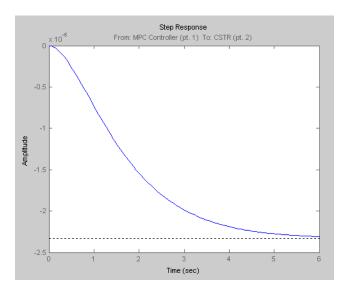


Rename Linearized Model to Plant1 as shown, clear the **Operating Point** check box (because there's no reason to export it), and click **OK**. This exports the linearized model as an LTI object named Plant1.

At the MATLAB command line, type:

step(Plant1)

You should obtain the following plot.



Thus, the linearized model predicts that a unit step *increase* in the coolant temperature will *decrease* the residual concentration, which is qualitatively correct. (Increasing the coolant temperature increases the reactor temperature. This increases the reaction rate, and the residual concentration decreases.)

The predicted magnitude is very small, however: of order  $10^{-6}$ . It should be of order  $10^{-2}$  (you can verify this by removing the controller block from the diagram and running an open-loop step-response simulation). The incorrect assumptions used to generate the default operating point are the cause. If this incorrect model were used in the controller, the coolant-temperature adjustments would be far too large, probably resulting in unstable behavior.

# **Modifying the Linearized Model**

Therefore, the next step is to define a reasonable operating point and calculate a corresponding linearized model.

In the navigation tree, click the MPC Task - MPC Controller node. Notice that the nominal input and output signal values are zero by default. As discussed in "Using Simulink® Control Design™ to Linearize Simulink Model" on page 2-14, the plant is at steady state at a coolant temperature of 298.15 K and a residual concentration of 8.57 kmol/m³. Thus, in the Input signal properties table, set the coolant temperature's nominal value to 298.15, as shown below, and in the Output signal properties table, set the concentration's nominal value to 8.57. Also assign more descriptive signal names, as shown.

Name	Туре	Description	Units	Nominal
Coolant Temperature	Manipulated			298.15
Output signal prop	perties —			
Output signal prop	rerties Type	Description	Units	Nominal
Name	,	Description	Units	Nominal 8.57
	Туре	Description	Units	
Name	Туре	Description	Units	
Name	Туре	Description	Units	

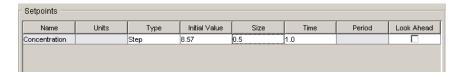
Click the **Import Plant** button to open the Plant Model Importer dialog box. Then do the following:

- 1 Click the Linearized Plant from Simulink tab.
- **2** Change the **Linearization model name** to Plant2.
- **3** Select **Create a new operating condition from MPC I/O values**, and then click **OK**. A new model node named **Plant2** and its operating point will appear within your design task. Verify that its actual dx values are now all close to zero and the outputs are essentially equal to their desired values.
- **4** Expand the **Controllers** node to expose the **MPC1** node and select it. On its **Model and Horizons** pane, set **Plant model** to Plant2. This replaces the default (invalid) model with the modified one.

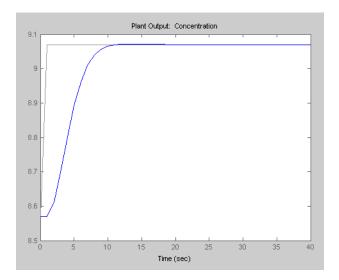
Leave the other controller settings at their default values.

### **Linear Simulation Tests**

It's good practice to test a controller in linear simulations before trying it on the nonlinear plant. Expand the **Scenarios** node and select **Scenario1**. Set **Plant** to Plant2, and set **Duration** to 40. Finally, define a step increase of 0.5 units in the concentration setpoint starting at time t = 1, as shown below.



Click the scenario's **Simulate** button. This linear test predicts a smooth, rapid approach to the new setpoint with minimal overshoot, as shown below.



The corresponding coolant temperature adjustments are reasonable (not shown). If anything, you might want to make the controller more aggressive by adjusting its tuning weights (see "Weight Tuning" on page 3-20).

**Note** This plant's steady-state gain is of order 0.01. Therefore, the default tuning weights lead to a relatively sluggish response. In general, you must adjust the tuning weights to compensate for the plant's natural input/output response magnitudes.

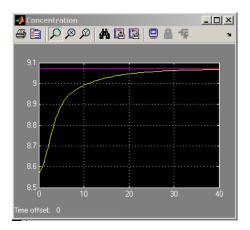
You can also run tests to verify that the controller responds rapidly to either of the two unmeasured disturbances (not shown).

### **Nonlinear Simulation Tests**

The controller seems to be performing well in linear tests, so try it with the nonlinear plant. As will be demonstrated below, you can run simulations that automatically use your latest design from the design tool. If the performance is unsatisfactory, you can easily change your design and retest.

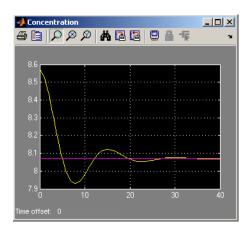
In the CSTR\_MPC model window, change the concentration setpoint to 9.07. This simulates a 0.5-unit step increase in the setpoint at time t = 0. Run the

Simulink simulation. The MPC Controller block automatically obtains the most recent MPC1 definition from the design tool. If necessary, open the model's concentration scope block. The result should be as shown below.



The nonlinear response is more sluggish than the linear prediction. The controller reduces the coolant temperature to about 284.6 K (verify this by opening the model's coolant temperature scope), whereas the linear simulation predicts a reduction to 289.4 K. In other words, when plant moves in this direction, the linearized model's gain is too large. Still, the concentration goes to the setpoint rapidly.

Next, set the concentration setpoint to 8.07, i.e., a step-change of equal magnitude in the opposite direction. Run the simulation to obtain the concentration scope response shown below.



In this direction, the response is underdamped. You can verify that the controller changes the coolant temperature to 304.1 K, an increase of 6.0 K (recall the decrease of 13.5 K when the change was in the opposite direction). In other words, the controller's linear model underpredicts the effect of a coolant temperature increase. If the setpoint were reduced significantly, the closed-loop system would become unstable (try 7.0, for example).

Thus, the controller's effective operating range is limited. If you wanted to operate at a low concentration, you'd need to determine a linearized model at that condition and use it to design another controller.

**Note** This is typical of strongly nonlinear plants. If you needed to operate a conventional controller over such a wide range, you might consider gain scheduling. Equivalently, you could define predictive controllers for several operating points and switch from one to another depending on the measured concentration (see "Simulations Involving Nonlinear Plants" on page 4-9 for an example of this).

For the tested range, however, the oscillations die out quickly. You can verify that the controller responds equally well to small, sustained disturbances (i.e.,  $\pm 0.5$  in feed concentration or  $\pm 3$  in feed temperature.

## Modifying the Controller Using the Design Tool

Keeping the design tool open makes it easy to test controller modifications. Each time you run a Simulink simulation, the MPC Controller block automatically obtains the latest settings for its MPC controller parameter (MPC1 in the above tests).

It's also easy to compare several controllers. Suppose you wanted to try a different control interval (the controller designed above uses a 1-second interval). Create a new controller by right-clicking the design tool's MPC1 controller node, and selecting Copy Controller in the menu. This creates a duplicate controller called MPC1\_copy. Rename it MPC2. Select MPC2 in the tree, activate its Model and Horizons tab and set Control interval to 2.

Now return to the MPC Controller block mask (if necessary, double-click the block to open the mask) and change **MPC controller** from MPC1 to MPC2. Close the mask or click the **Apply** button to notify the controller of this change. Run a simulation with a disturbance or setpoint change, and then open the **Coolant Temperature** scope. You should see that the controller is now making step-wise adjustments every 2 minutes. As would be expected, controller performance degrades with less frequent measurement feedback, but not much in this case.

To restore the original controller, just change MPC2 to MPC1 in the block mask and click **Apply**.

# **Exiting the Design Tool**

When you close the design tool, you'll be prompted to save any projects you've created or edited. For details, see "Saving a Project" on page 3-66.

Once the design tool has closed, the MPC Controller block mask expects its controller object to be in your workspace. Thus, you'll also be prompted to export such controller objects. You need to do this if you plan to run your Simulink model after you've closed the design tool.

# **Saving Your Work**

You'll usually want to save your design so you can reuse or revise it. You can save individual controllers or an entire project.

When you close the design tool, you'll be prompted to save new or modified designs. You can also save manually to preserve an intermediate state or guard against an unexpected shutdown.

This section covers the following topics:

- "Exporting a Controller" on page 3-65
- "Saving a Project" on page 3-66

#### **Exporting a Controller**

To save a controller, *export* it to your MATLAB workspace or to a MAT-file. The former allows you to use the exported controller in command-line functions or a Simulink block.

**Note** Your workspace disappears when you exit MATLAB. A MAT-file is permanent, and you can reload it in a subsequent MATLAB session.

The following example assumes that the design tool is open and in the state described in the previous section. Suppose you want to export the controller to your workspace. Expand the tree if necessary, right-click **MPC2**, and select **Export Controller** from the resulting menu. The following dialog box appears.



The default behavior is to export the selected controller to the workspace. Click **Export** to confirm. You can verify the export by typing

#### whos

at the MATLAB prompt. The resulting list should include an  $\ensuremath{\mathtt{mpc}}$  object named MPC2. Type

#### MPC2

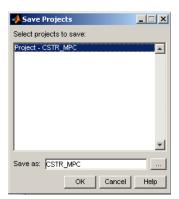
to display the object's properties.

#### Saving a Project

To save your entire project, click the toolbar's **Save** button.



The following dialog box appears.



#### Dialog Box for Saving a Controller Design Project

The default behavior saves the current project (named Project - CSTR\_MPC in this case) in a MAT-file (called CSTR\_MPC here). If the design tool had contained other projects, they would appear in the list, and you could select the ones you wanted to save.

The MAT-file will be saved in the default folder. To verify the location, click the **Browse (...)** button and change the folder if necessary. When ready to save, click **OK**.

# **Loading Your Saved Work**

The following assumes that you've saved a project as described in the previous section. To reload this project, close the design tool if it's open. Also clear any mpc objects from your workspace. (Type whos at the MATLAB prompt for a list of objects.) For example, if MPC1 and MPC2 are in your workspace, type

clear MPC1 MPC2

to clear (remove) them.

If you've closed the CSTR\_MPC model, open it. (Simulink Model for CSTR Control on page 3-54 shows the model diagram). Double-click the MPC Controller block to open its mask, and verify that the **MPC Controller** parameter is set to MPC2.

**Note** If you were to attempt to run the CSTR\_MPC model at this stage, an error dialog box would indicate that the MPC Controller block was unable to initialize. The MPC2 object specified in the block mask must be loaded into your workspace or be part of an active design tool task.

You could define the required MPC2 object in one of the following ways:

- Import MPC2 from a MAT-file (assuming you had saved it as explained in "Exporting a Controller" on page 3-65).
- Load the model's project file, which contains a copy of MPC2.

To use the second approach, open the design tool by typing

mpctool

in the MATLAB Command Window. This creates a blank Model Predictive Control Toolbox project called **MPC Design Task**. Click **Load** on the toolbar.



This opens a dialog box similar to that shown in Dialog Box for Saving a Controller Design Project on page 3-67. Use it to select the project file you've saved, and then click **OK** to load the project. It should appear in the tree. Verify that it contains a controller named MPC2.

Run the CSTR\_MPC model in Simulink. The block mask automatically retrieves MPC2 from the design tool, and the simulation runs. In other words, loading the project automatically restores the link between the design tool and the MPC Controller block.

# Designing Controllers Using the Command Line

- "Controller Definition" on page 4-2
- "Linear Simulations" on page 4-7
- "Simulations Involving Nonlinear Plants" on page 4-9
- "Control Based On Multiple Plant Models" on page 4-14
- "Analysis Tools" on page 4-22
- "Bibliography" on page 4-25

#### **Controller Definition**

Chapter 3, "Designing Controllers Using the Design Tool GUI" showed how to use the Model Predictive Control Toolbox design tool to create a controller and test it. You might prefer to use functions instead. They allow access to options not available in the design tool, as well as automation of repetitive tasks using scripts and customized plotting.

This section covers the following topics:

- "Creating a Controller Object" on page 4-2
- "Viewing and Altering Controller Properties" on page 4-3

#### **Creating a Controller Object**

The following uses the CSTR model described in Chapter 2, "Building Models" as an example. To follow along, verify that the model's LTI object is in your MATLAB workspace (if necessary, create it as explained in "Chemical Reactor Example" on page 2-5, and set its label and signal type properties as explained in "LTI Properties for the CSTR Example" on page 2-7).

Use the mpc function to create a controller. For example, type

```
Ts = 1;
MPCobj = mpc(CSTR, Ts);
```

to create one based on the CSTR model with a control interval of 1 time unit and all other parameters at their default values.

**Note** MPCobj is an MPC object. It contains a complete controller definition for use with Model Predictive Control Toolbox software.

To display the controller's properties in the Command Window, type

```
display(MPCobj)
```

or type the object's name without a trailing semicolon.

#### **Viewing and Altering Controller Properties**

Once you've defined an MPC object, it's easy to alter its properties. For a description of the editable properties, type:

```
mpcprops
```

To display the list of properties and their current values, type

```
get(MPCobj)
```

For the CSTR example this displays:

(Your History entry will differ.) To alter one of these properties, you can use the syntax

```
ObjName.PropName = value;
```

where ObjName is the object name, and PropName is the property you want to set. For example, to change the prediction horizon from 10 (the default) to 15, type:

```
MPCobj.P = 15;
```

**Note** You can abbreviate property names provided that the abbreviation is unambiguous.

As shown above, many of the properties are MATLAB structures containing additional properties. For example, type

MPCobj.MV

which displays:

```
Min: -Inf
       Max: Inf
    MinECR: 0
    MaxECR: 0
   RateMin: -Inf
   RateMax: Inf
RateMinECR: 0
RateMaxECR: 0
    Target: 'nominal'
      Name: 'T c'
     Units: ''
```

This shows that the default controller has no constraints on the manipulated variable. To include constraints as shown in Entering CSTR Manipulated Variable Constraints on page 3-30, you could type

```
MPCobj.MV.Min = -10;
MPCobj.MV.Max = 10;
MPCobj.MV.RateMin = -4;
MPCobj.MV.RateMax = 4;
MPCobj.MV.Units = 'Deg C';
or use the set command:
set(MPCobj, 'MV', struct('Min', -10, 'Max', 10, ...
 'RateMin', -4, 'RateMax', 4, 'Units', 'Deg C'));
```

**Note** The Units property is for display purposes only and is optional.

There are two outputs in this case, so MPCobj.OV is a 1-by-2 structure. To set measurement units to the values shown in Controller Options — Weight Tuning Tab on page 3-20, you could type

```
MPCobj.OV(1).Units = 'Deg C';
MPCobj.OV(2).Units = 'kmol/m^3';
```

Finally, check the default weights by typing

MPCobj.W

which displays:

```
ManipulatedVariables: 0
ManipulatedVariablesRate: 0.1000
OutputVariables: [1 1]
ECR: 100000
```

Change to the values shown in Controller Options — Weight Tuning Tab on page 3-20 by typing:

```
MPCobj.W.ManipulatedVariablesRate = 0.3;
MPCobj.W.OutputVariables = [1 0];
```

You can also specify time-varying weights and constraints. The time-varying weights and constraints are defined for the prediction horizon, which shifts at each time step. This implies that as long as the property is not changed, the set of time-varying parameters is the same at each time step. Type mpcprops or see the User's Guide for details. To learn how to specify time-varying constraints and weights in the GUI, see "Constraints Tab" and "Weight Tuning Tab" in the *Model Predictive Control Toolbox User's Guide*.

The time-varying weights modify the tuning of the unconstrained controller response. To specify a different weight for each step in the prediction horizon, modify the Weightproperty. For example,

```
MPCobj.W.OutputVariables = [0.1 0; 0.2 0; 0.5 0; 1 0];
```

deemphasizes setpoint tracking errors early in the prediction horizon. The default weight of 1 is used for the fourth step and beyond.

Constraints can also be time varying. The time-varying constraints have a nonlinear effect when they are active. For example,

```
MPCobj.MV.RateMin=[-4;-3.5;-3;-2.5]
MPCobj.MV.RateMax=[4;3.5;3;2.5]
```

forces MV to change more and more slowly along the prediction horizon. The constraint of -2.5 and 2.5 is used for the fourth step and beyond.

You could also alter the controller's disturbance rejection characteristics using functions that parallel the design tool's disturbance modeling options (described in "Disturbance Modeling and Estimation" on page 3-31). See the reference pages for the setestim, setindist, and setoutdist functions.

#### **Linear Simulations**

Model Predictive Control Toolbox functions allow you to perform linear closed-loop and open-loop simulations. This section covers the following topics:

- "Using the sim Function" on page 4-7
- "Saving Calculated Results" on page 4-7
- "Simulation Options" on page 4-8

#### Using the sim Function

To run a linear simulation, use the sim function. For example, given the MPCobj controller defined in the previous section, type:

```
T = 26;
r = [2 0];
sim(MPCobj, T, r);
```

This simulates the closed-loop response for a duration of 26 control intervals with a setpoint of 2 for the first output (the reactor temperature) and 0 for the second output (the residual concentration). Recall that the second output's tuning weight is zero (see the discussion in "Output Weights" on page 3-22), so its setpoint is ignored.

By default, the same linear model is used for controller predictions and the plant, i.e., there is no plant/model mismatch. You can alter this as shown in "Simulation Options" on page 4-8.

When you use the above syntax (no output variables), sim automatically plots the plant inputs and outputs (not shown, but see Improved Setpoint Tracking for CSTR Temperature on page 3-21 and Plant Inputs for Modified Rate Weight on page 3-24 for results of a similar scenario).

#### **Saving Calculated Results**

If you'd like to save simulation results in your workspace, use the following sim function format:

```
[y, t, u] = sim(MPCobj, T, r);
```

This suppresses automatic plotting, instead creating variables y, t, and u, which hold the computed outputs, time, and inputs, respectively. A typical use is to create customized plots. For example, to plot both outputs on the same axis versus time, you could type:

```
plot(t, y)
```

#### **Simulation Options**

You can modify simulation options using the mpcsimopt function. For example, the code

```
MPCopts = mpcsimopt;
MPCopts.Constraints = 'off';
sim(MPCobj, T, r, MPCopts)
```

runs an unconstrained simulation. Comparing to the case described in "Using the sim Function" on page 4-7, the controller's first move is now exceeds 4 units (the specified rate constraint).

Other options include the addition of a specified noise sequence to the manipulated variables or measured outputs, open-loop simulations, a look-ahead option for better setpoint tracking or measured disturbance rejection, and plant/model mismatch.

For example, the following code defines a new plant model having gains 50% larger than those in the CSTR model used in the controller, then repeats the above simulation:

```
Plant = 1.5*CSTR;
MPCopts.Model = Plant;
sim(MPCobj, T, r, MPCopts)
```

In this case, the plant/model mismatch degrades controller performance, but only slightly. Degradation can be severe and must be tested on a case-by-case basis.

## Simulations Involving Nonlinear Plants

You can also use sim to simulate a closed-loop system consisting of a linear plant model and an MPC controller.

If your plant is a nonlinear Simulink model, you must linearize the plant (see "Linearization Using Linear Analysis Tool in Simulink Control Design" on page 2-17) and design a controller for the linear model (see "Nonlinear Plants" on page 3-53). To simulate the system, specify the controller in the MPC block parameter **MPC Controller** field and run the closed-loop Simulink model.

Alternatively, your nonlinear model might be a MEX-file, or you might want to include features unavailable in the MPC block, such as a custom state estimator. The mpcmove function is the Model Predictive Control Toolbox computational engine, and you can use it in such cases. The disadvantage is that you must duplicate the infrastructure that the sim function and the MPC block provide automatically.

The rest of this section covers the following topics:

- "Nonlinear CSTR Application" on page 4-9
- "Example Code for Successive Linearization" on page 4-10
- "CSTR Results and Discussion" on page 4-11

#### **Nonlinear CSTR Application**

The CSTR model described in "Using Simulink® Control Design™ to Linearize Simulink Model" on page 2-14 is a strongly nonlinear system. As shown in "Nonlinear Plants" on page 3-53, a controller can regulate this plant, but degrades (and might even become unstable) if the operating point changes significantly.

The objective of this example is to redefine the predictive controller at the beginning of each control interval so that its predictive model, though linear, represents the latest plant conditions as accurately as possible. This will be done by linearizing the nonlinear model repeatedly, allowing the controller to adapt as plant conditions change. See references [1] and [2] for more details on this approach.

#### **Example Code for Successive Linearization**

In the following code, the simulation begins at the CSTR model's nominal operating point (concentration = 8.57) and moves to a low concentration (= 2) where the reaction rate is much higher. The required code is as follows:

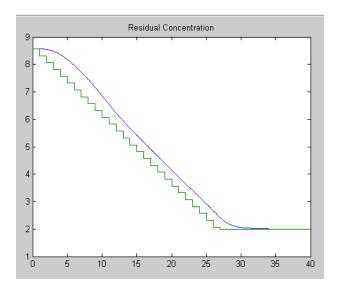
```
[sys, xp] = CSTR INOUT([],[],[],'sizes');
up = [10 298.15 298.15];
u = up(3);
tsave = []; usave = []; ysave = []; rsave = [];
Ts = 1;
t = 0;
while t < 40
    yp = xp;
    % Linearize the plant model at the current conditions
    [a,b,c,d]=linmod('CSTR INOUT', xp, up );
    Plant = ss(a,b,c,d);
    Plant.InputGroup.ManipulatedVariables = 3;
    Plant.InputGroup.UnmeasuredDisturbances = [1 2];
    Model.Plant = Plant;
    % Set nominal conditions to the latest values
    Model.Nominal.U = [0 0 u];
    Model.Nominal.X = xp;
    Model.Nominal.Y = vp;
    dt = 0.001;
    Options = simset('InitialState', xp);
    [T, XP, YP] = sim('CSTR INOUT', [t t+dt], Options, ...
        [t up; t+dt up]);
    Model.Nominal.DX = (1/dt)*(XP(end,:)' - xp(:));
    % Define MPC Toolbox controller for the latest model
    MPCobj = mpc(Model, Ts);
    MPCobj.W.Output = [0 1];
    % Ramp the setpoint
    r = max([8.57 - 0.25*t, 2]);
    % Compute the control action
    if t <= 0
        xd = [0; 0];
        x = mpcstate(MPCobj, xp, xd, [], u);
    end
    u = mpcmove(MPCobj, x, yp, [0 r], []);
    % Simulate the plant for one control interval
```

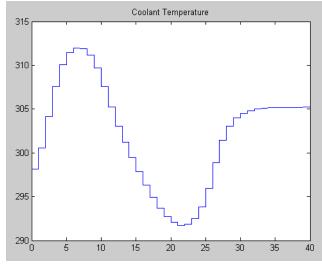
```
up(3) = u;
    Options = simset('InitialState', xp);
    [T, XP, YP] = sim('CSTR INOUT', [t t+Ts], Options, ...
        [t up; t+Ts up]);
    % Save results for plotting
    tsave = [tsave; T];
    ysave = [ysave; YP];
    usave = [usave; up(ones(length(T),1),:)];
    rsave = [rsave; r(ones(length(T),1),:)];
    xp = XP(end,:)';
    t = t + Ts;
end
figure(1)
plot(tsave,[ysave(:,2) rsave])
title('Residual Concentration')
figure(2)
plot(tsave, usave(:,3));
title('Coolant Temperature')
```

#### **CSTR Results and Discussion**

The plotted results appear below. Note the following points:

- The setpoint is being ramped from the initial concentration to the desired final value (see the step-wise changes in the reactor concentration plot below). The reactor concentration tracks this ramp smoothly with some delay (see the smooth curve), and settles at the final state with negligible overshoot. The controller works equally well (and achieves the final concentration more rapidly) for a step-wise setpoint change, but it makes unrealistically rapid changes in coolant temperature (not shown).
- The final steady state requires a coolant temperature of 305.20 K (see the coolant temperature plot below). An interesting feature of this nonlinear plant is that if one starts at the initial steady state (coolant temperature = 298.15 K), stepping the coolant temperature to 305.20 and holding will not achieve the desired final concentration of 2. In fact, under this simple strategy the reactor concentration stabilizes at a final value of 7.88, far from the desired value. A successful controller must increase the reactor temperature until the reaction "takes off," after which it must reduce the coolant temperature to handle the increased heat load. The relinearization approach provides such a controller (see following plots).





- Function linearize relinearizes the plant as its state evolves. This function was discussed previously in "Linearization Using MATLAB Code" on page 2-14.
- The code also resets the linear model's nominal conditions to the latest values. Note, however, that the first two input signals, which are

unmeasured disturbances in the controller design, always have nominal zero values. As they are unmeasured, the controller cannot be informed of the true values. A non-zero values would cause an error.

- Function mpc defines a new controller based on the relinearized plant model. The output weight tuning ignores the temperature measurement, focusing only on the concentration.
- At t = 0, the mpcstate function initializes the controller's extended state vector, x, which is an *mpcstate object*. Thereafter, the mpcmove function updates it automatically using the controller's default state estimator. It would also be possible to use an Extended Kalman Filter (EKF) as described in [1] and [2], in which case the EKF would reset the mpcstate input variables at each step.
- The mpcmove function uses the latest controller definition and state, the measured plant outputs, and the setpoints to calculate the new coolant temperature at each step.
- The Simulink sim function simulates the nonlinear plant from the beginning to the end of the control interval. Note that the final condition from the previous step is being used as the initial plant state, and that the plant inputs are being held constant during each interval.

Remember that a conventional feedback controller or a fixed Model Predictive Control Toolbox controller tuned to operate at the initial condition would become unstable as the plant moves to the final condition. Periodic model updating overcomes this problem automatically and provides excellent control under all conditions.

#### **Control Based On Multiple Plant Models**

The "Nonlinear CSTR Application" on page 4-9 shows how updates to the prediction model can improve MPC performance. In that case the model is nonlinear and you can obtain frequent updates by linearization.

A more common situation is that you have several linear plant models, each of which applies at a particular operating condition and you can design a controller based on each linear model. If the models cover the entire operating region and you can define a criterion by which you switch from one to another as operating conditions change, the controller set should be able to provide better performance than any individual controller.

The Model Predictive Control Toolbox includes a Simulink block that performs this function. It is the *Multiple MPC Controllers* block. The rest of this section is an illustrative example organized as follows:

- "A Two-Model Plant" on page 4-14
- "Designing the Two Controllers" on page 4-16
- "Simulating Controller Performance" on page 4-17

#### **A Two-Model Plant**

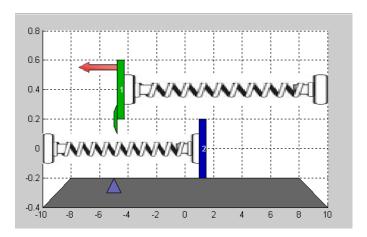
**Note** The demo Switching MPC Controllers with Multiple MPC Controllers Block provides an animated version of the plant described below.

Animation of the Multi-Model Example on page 4-15 is a stop-action snapshot of the subject plant. It consists of two masses,  $M_1$  and  $M_2$ . A spring connects  $M_1$  to a rigid wall and pulls it to the right. An applied force, shown as a red arrow in Animation of the Multi-Model Example on page 4-15, opposes this spring, pulling  $M_1$  to the left.

When the two masses are detached, as in Animation of the Multi-Model Example on page 4-15, mass  $\rm M_2$  is uncontrollable and responds only to the spring pulling it to the left.

If the two masses collide, however, they stick together (the collision is completely inelastic) until a change in the applied force separates them.

The control objective is to move  $M_1$  in response to a command signal. The blue triangle in Animation of the Multi-Model Example on page 4-15 represents the desired location. At the instant shown, the desired location is -5.



#### **Animation of the Multi-Model Example**

In order to achieve its objective, the controller can adjust the applied force magnitude (the length of the red arrow). It receives continuous feedback on the  $M_1$  location. There is also a contact sensor to signal collisions. The  $M_2$  location is unmeasured.

If  $M_1$  were isolated, this would be a routine control problem. The challenge is that the relationship between the applied force and the  $M_1$  movement changes dramatically when  $M_2$  attaches to  $M_1$ .

The following code defines the model. First define the system parameters as follows:

```
%% Model Parameters
M1=1; % mass
M2=5; % mass
k1=1; % spring constant
k2=0.1; % spring constant
```

```
% friction coefficient
b1=0.3;
b2=0.8;
            % friction coefficient
yeq1=10;
            % wall mount position
yeq2=-10;
            % wall mount position
```

Next define a model of M<sub>1</sub> when the masses are separated. Its states are the M<sub>1</sub> position and velocity. Its inputs are the applied force, which will be the controller's manipulated variable, and a spring constant calibration signal, which is a measured disturbance input.

```
A1=[0 1;-k1/M1 -b1/M1];
B1=[0 \ 0; -1/M1 \ k1*yeq1/M1];
C1=[1 \ 0];
D1=[0\ 0];
sys1=ss(A1,B1,C1,D1);
sys1=setmpcsignals(sys1, 'MV', 1, 'MD', 2);
```

The setmpcsignals command specifies the input type for the two inputs.

We need another model (with the same input/output structure) to predict movement when the two masses are joined, as follows:

```
A2=[0 1; -(k1+k2)/(M1+M2) -(b1+b2)/(M1+M2)];
B2=[0 0; -1/(M1+M2) (k1*yeq1+k2*yeq2)/(M1+M2)];
C2=[1 \ 0];
D2=[0\ 0];
sys2=ss(A2,B2,C2,D2);
sys2=setmpcsignals(sys2, 'MV', 1, 'MD', 2);
```

#### **Designing the Two Controllers**

Next we define controllers for each case. Both use a 0.2 second sampling period, a prediction horizon of P = 20, a control horizon of M = 1, and the default values for all other controller design parameters. The only difference in the controllers is the prediction model.

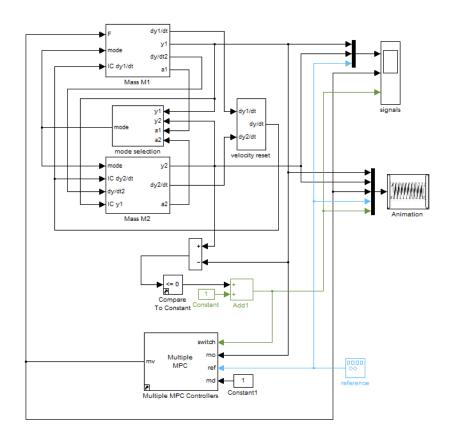
```
Ts=0.2;
            % sampling time
p=20;
            % prediction horizon
            % control horizon
m=1;
MPC1=mpc(sys1,Ts,p,m); % Controller for M1 detached from M2 MPC2=mpc(sys2,Ts,p,m); %
Controller for M1 connected to M2
```

The applied force also has the same constraints in each case. Its lower bound is zero (it can't reverse direction), and its maximum rate of change is 1000 per second (increasing or decreasing).

```
MPC1.MV=struct('Min',0,'RateMin',-1e3,'RateMax',1e3);
MPC2.MV=struct('Min',0,'RateMin',-1e3,'RateMax',1e3);
```

#### **Simulating Controller Performance**

Block Diagram of the Two-Model Example on page 4-18 shows the Simulink block diagram for this example. The upper portion simulates the movement of the two masses, plots the signals as a function of time, and animates the demo.



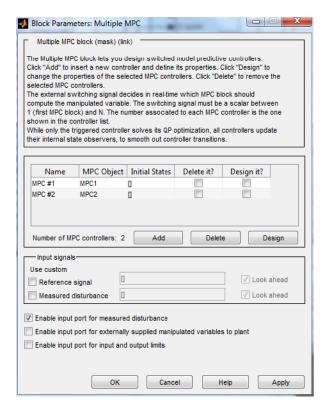
#### **Block Diagram of the Two-Model Example**

The lower part contains three key elements:

- A pulse generator that supplies the desired M<sub>1</sub> position (the controller reference signal). Its output is a square wave varying between -5 and 5 with a frequency of 0.015 per second.
- A simulation of a contact sensor. When the two masses have the same position, the Compare to Constant block evaluates to true, and the Add1 block converts this to a 2. Otherwise, the Add1 output is 1.
- The Multiple MPC Controller block. It has four inputs. The measured output (mo), reference (ref), and measured disturbance (md) inputs are as

for a standard MPC Controller block. The distinctive feature is the switch input.

The figure below shows the Multiple MPC Controller block mask for this example (obtained by double clicking on the controller block).



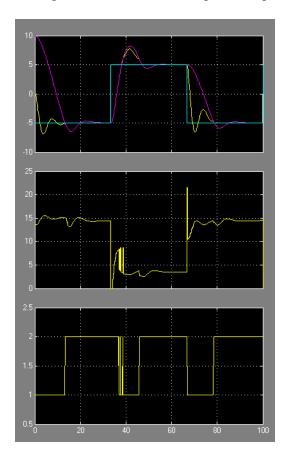
When the switch input is 1 the block automatically activates the first controller listed (MPC1), which is appropriate when the masses are separated. When the switch input is 2 the block automatically enables the second controller (MPC2).

The following code simulates the controller performance

```
Tstop=100; % Simulation time y1initial=0; % Initial M1 and M2 Positions
```

```
y2initial=10;
open('mpc switching');
sim('mpc_switching',Tstop);
```

The figure below shows the signals scope output.



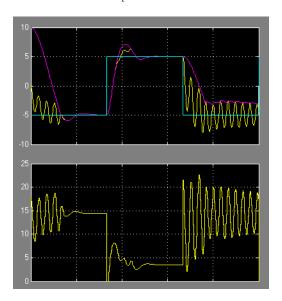
In the upper plot, the cyan curve is the desired position. It starts at -5. The M<sub>1</sub> position (yellow) starts at 0 and under the control of MPC1, M<sub>1</sub> moves rapidly toward the desired position.  $M_2$  (magenta) starts at 10 and begins moving in the same direction. At about t = 13 seconds,  $M_2$  collides with  $M_1$ . The switching signal (lower plot) changes at this instant from 1 to 2, so controller MPC2 has taken over.

The collision moves  $M_1$  away from its desired position and  $M_2$  remains joined to  $M_1$ . Controller MPC2 adjusts the applied force (middle plot) so  $M_1$  quickly returns to the desired position.

When the desired position changes step-wise to 5, the two masses separate briefly (with appropriate switching to MPC1) but for the most part move together and settle rapidly at the desired position. The transition back to -5 is equally well behaved.

Now suppose we force MPC2 to operate under all conditions. The figure below shows the result. When the masses are separated, as at the start, MPC2 applies excessive force and then over-compensates, resulting in oscillatory behavior. Once the masses join, the movement smooths out, as would be expected.

The oscillations are especially severe in the last transition. The masses collide frequently and  $M_1$  never reaches the desired position.



If we put MPC1 in charge exclusively, we instead see sluggish movements that fail to settle at the desired position before the next transition occurs. (not shown but you can run the mpcswitching demo).

In this case, at least, two controllers are better than one.

# **Analysis Tools**

The are many ways to analyze a controller design. This section highlights two functions that support analysis of Model Predictive Control Toolbox controllers:

- "Steady-State Gain Computation" on page 4-22
- "Controller Extraction" on page 4-23

#### **Steady-State Gain Computation**

The cloffset function computes the closed-loop, steady-state gain for each output when subjected to a sustained, 1-unit disturbance added to each output. It assumes that no constraints will be encountered.

For example, consider the controller operating at the final steady-state of the nonlinear CSTR of the previous section. To compute its gain, type

```
which gives the result:
ans =
               14.5910
    1.0000
   -0.0000
               -0.0000
```

cloffset(MPCobj)

The interpretation is that the controller doesn't react to a sustained disturbance of 1 unit in the first output (the reactor temperature). Recall that we assigned zero weight to this output in the controller design, so the controller ignores deviations from its setpoint. The same disturbance has no effect on the second output (the 2,1 element is zero).

If there is a 1-unit disturbance in the second output, the controller reacts, and the first output increases 14.59 units. This is again due to the zero weight on this output. The second output stays at its setpoint (the 2,2 element is zero).

#### **Controller Extraction**

Use the ss function to obtain an LTI representation of an unconstrained Model Predictive Control Toolbox controller. You can use this to analyze the controller's closed-loop frequency response, etc.

For example, consider the controller designed in "Creating a Controller Object" on page 4-2. To extract the controller, you could type:

```
MPCss = ss(MPCobj);
```

You could then construct an LTI model of the closed-loop system using the feedback function (see the Control System Toolbox documentation for details) by typing:

```
CSTRd = c2d(CSTR, MPCss.Ts);
Feedin = 1;
Feedout = 1;
Sign = 1;
CLsys = feedback(CSTRd, MPCss, Feedin, Feedout, Sign);
```

**Note** The CSTR model must be converted to discrete form with the same control interval as the controller.

Recall that the CSTR plant has two inputs and two outputs. The first input is the manipulated variable and the other is an unmeasured disturbance. The first output is measured for feedback and the other is not. The Feedin and Feedout parameters specify the input and output to be used for control. The Sign parameter signifies that the MPC object uses positive feedback, i.e., the measured outputs enter the controller with no sign change. Omission of this would cause the feedback command to use negative feedback by default and would almost certainly lead to an unstable closed-loop system.

You could then type

```
eig(CLsys)
```

to verify that all closed-loop poles are within the unit circle, or

bode(CLsys)

to compute a closed-loop Bode plot.

# **Bibliography**

- [1] Lee, J. H. and N. L. Ricker, "Extended Kalman Filter Based Nonlinear Model Predictive Control," *Ind. Eng. Chem. Res.*, Vol. 33, No. 6, pp. 1530–1541 (1994).
- [2] Ricker, N. L., and J. H. Lee "Nonlinear Model Predictive Control of the Tennessee Eastman Challenge Process," *Computers & Chemical Engineering*, Vol. 19, No. 9, pp. 961–981 (1995).

# Designing and Testing Controllers in Simulink

- "Designing a Model Predictive Controller for a Plant" on page 5-2
- "Testing an Existing Controller" on page 5-17
- "Coordination of Multiple Model Predictive Controllers" on page 5-18

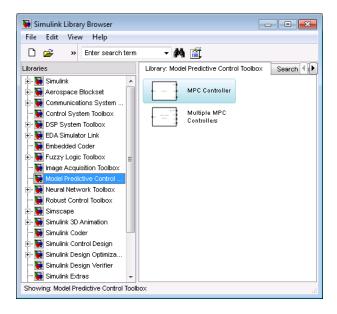
The Model Predictive Control Toolbox provides a controller block library for use in Simulink. This allows you to test controller performance in nonlinear simulations. The procedure depends on whether you have already designed a controller. You also have the option to coordinate multiple Model Predictive Controllers.

## **Designing a Model Predictive Controller for a Plant**

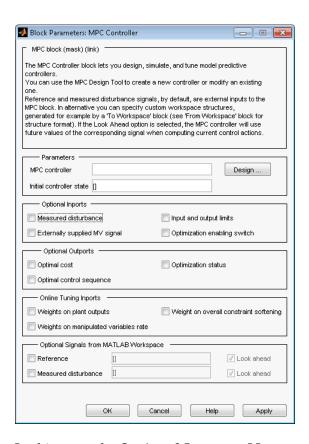
If you have a Simulink plant that needs a Model Predictive Controller:

- 1 Open the Simulink model.
- **2** Add an MPC Controller block to your Simulink model and connect it to the plant.

First, open the Simulink Library Browser and select the MPC Controller

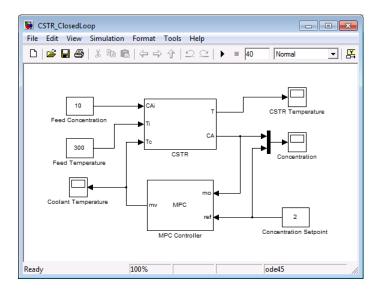


Drag and drop the MPC Controller into your Simulink model. Double click the controller block to configure its options:



In this example, **Optional Inports> Measured disturbance** option is unchecked and the **MPC Controller** box is blank, indicating that no controller has been designed yet.

Consider the nonlinear CSTR model. See "Linearization Using MATLAB Code" on page 2-14 for a description of the process.



In the above diagram, the controller has been connected such that the residual concentration is the measured and controlled output variable (MO) and the coolant temperature is the manipulated variable (MV). The feed concentration and temperature are unmeasured disturbances and the reactor temperature is ignored. In practice, the reactor temperature is usually measured and controlled, but the configuration here presents a more challenging nonlinear control problem.

The desired CSTR concentration is 2 kmol/m<sup>3</sup> and the above model includes this constant reference signal. It also includes scope plots of the MV, OV (with reference), and CSTR temperature.

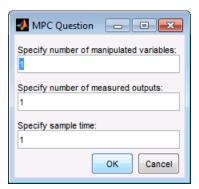
To open the model:

```
sys = 'CSTR_ClosedLoop';
open_model(sys);
```

**3** Initiate the controller design.

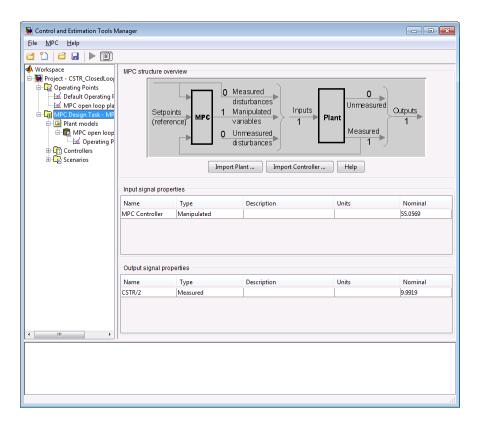
In the MPC Controller block, click **Design**.

This action opens the MPC Question dialog box that asks you for information about the plant.



In this case, there is one MV and one OV. We will use a controller sample time of 1 minute. Click **OK**.

This action opens the Control and Estimation Tools Manager window and linearizes the Simulink plant model. The linearization uses the signals connected to the controller. The Control and Estimation Tools Manager contains an **MPC Design Task** with the linearized plant model loaded in it.



The nominal values for the Input signal properties and Output signal properties are shown. In the MPC Design Task, select MPC open loop plant 1 to see the linearized prediction model.

**4** Evaluate the linearized plant model.

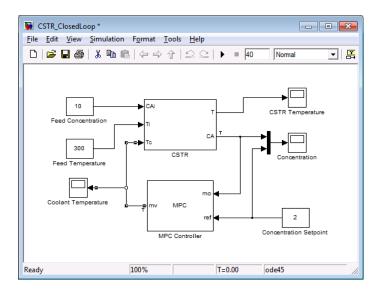
The automated linearization procedure uses the default equilibrium operating point that is likely different from the desired operating point. It is important to verify whether the operating point is appropriate. Else, the linear model may be unsuitable for model predictive control at the target conditions.

In the above figure, in the MPC Design Task, click Operating Point to see the default operating point. The linearization procedure is able to find a steady-state operating point (derivatives are close to zero), but it is far

from the target condition. The reactor temperature is very low (244 K) and consequently little reaction occurs — the concentration with the reactor is essentially equal to the feed concentration. Since the model has strong nonlinearities, the resulting linear model is probably a poor design basis.

- **5** If necessary, modify the operating point and re-linearize.
  - a Add output constraints.

In the Simulink model, right-click the MO signal entering the controller. Select **Linearization Points> Output constraint**. Repeat for the MV signal and measured disturbance (MD) signal of the MPC Controller block. When finished, all such signals should be marked with a **T** icon.



You must specify output constraints on all the OV/MV/MD signals connected to the MPC Controller because their steady-state values are used to compute the nominal values used by the model predictive controller.

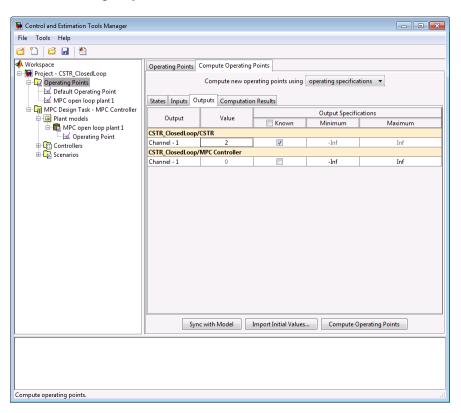
**b** Calculate a new operating point.

Return to the Control and Estimation Tools Manager. In the navigation pane, select **Operating Points**. Select the **Compute Operating Points** tab.

By default, the software computes a steady-state operating point.

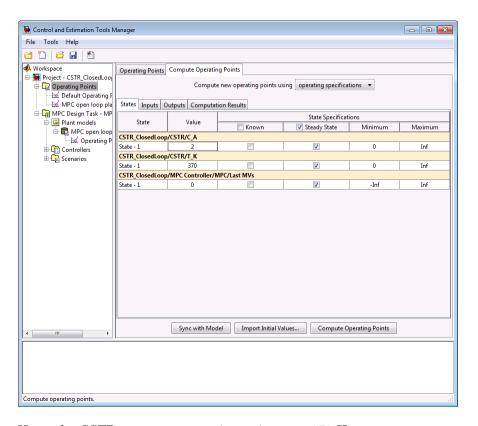
c Specify known outputs, if any.

The CSTR concentration must be 2 kmol/m<sup>3</sup>. Select the **Known** check box for it and specify 2 in the Value box.



**d** Supply initial estimates of the other states.

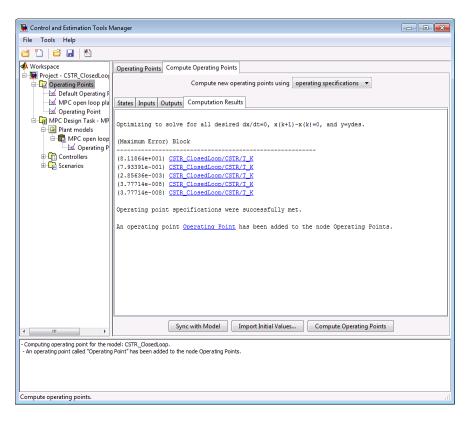
Otherwise, the numerical search for the new operating point may fail, depending on the plant's nonlinearity.



Here, the CSTR temperature estimate is set to 370 K.

**e** Calculate the new operating point.

Click **Compute Operating Points**. Ideally, the numerical search converges to the desired operating point and a message similar to the following appears:

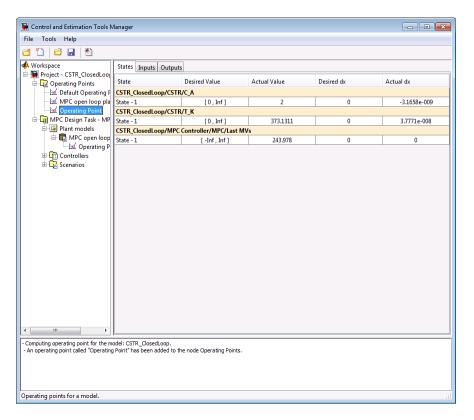


Note the name of the new operating point. It now appears in the navigation pane.

If the calculation fails, a message suggests that you revise the constraints you previously defined. You may also try supplying better initial estimates of the unknown quantities. You may also want to choose a different optimization algorithm for the operating point search. To specify a different optimization algorithm, in the Controls and Estimation Tools Manager, select **Options** in the **Tools** menu. Select **Operating Point Search**.

**f** Evaluate the new operating point.

Select the new operating point in the navigation pane.



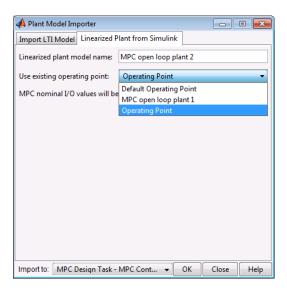
The new operating point is at steady state (all the derivatives are near zero). Also, the actual concentration value is 2 kmol/m³, as expect. Click the **Output** tabs to verify that the two outputs are consistent with the above.

**g** Linearize at the new operating point.

Select MPC Design Task in the navigation pane. Click Import Plant.

This action opens the Plant Model Importer dialog box.

Select the **Linearized Plant from Simulink** tab. Edit the name assigned to the new model and select the operating point on which the linearization is based.



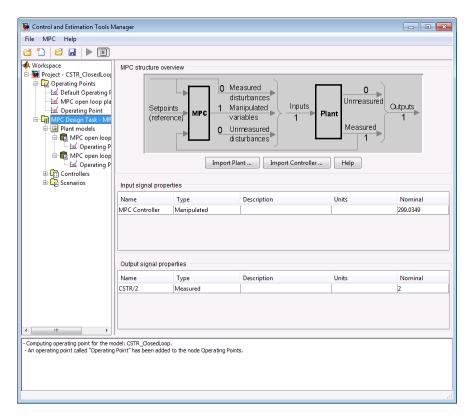
The above shows the Plant Model Importer dialog box after renaming the model to **MPC Rev1** and selecting **Operating Point**, which is the new operating point.

Click  $\mathbf{OK}$  to linearize the plant model. The new model will be installed in the MPC Design Task and its parameters will appear.

Click Close in the Plant Model Importer dialog box.

**h** Confirm the new plant model.

Select MPC Design Task in the navigation pane.



The above shows that the linearization procedure has entered the new nominal conditions. Note the MPC Design Task still contains both the new and the original models.

i (Optional) Delete the inappropriate model.

In the navigation pane, right-click the original model and select **Delete**. This forces the controller to use the new model and eliminates the potential for confusion.

**6** Export the controller to the Workspace.

By default, the MPC Design Task creates a controller based on the model obtained by automatic linearization. The default controller is named **MPC1**. The Control and Estimation Tools Manager automatically exports

it to the Workspace and enters the name MPC1 in the MPC Controller box of the MPC Controller block.

In general, you should use the design tool or commands to improve the design, testing initially with linear simulations. When finished with modifications, export the controller object to the Workspace. Right-click the controller in the navigation pane and select **Export**. You have the option to rename the controller when you export it.

**7** Verify steady state for the plant/controller combination.

The MPC Controller must contain the name of the controller that you want to use from the base workspace. In this example, you also need to export the new operating point and initialize the Simulink model with it.

Right-click Operating Point in mpc open loop plant 2 and select Export to workspace.

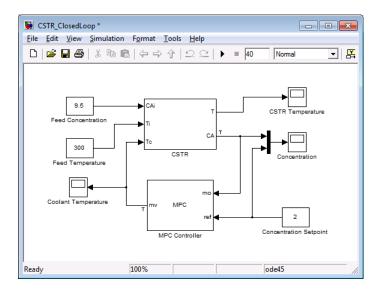
This action opens the Export to workspace dialog box.

Select the Use the operating point to initialize model check box.

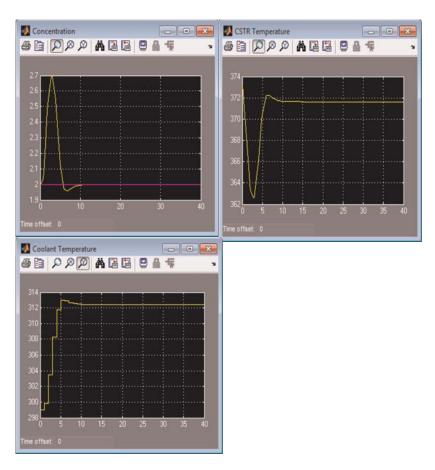
Run the Simulink model, including the installed controller to verify that both have been initialized to the correct nominal condition. If there are no disturbances, all signals would remain essentially constant. Else, make sure that the states within the plant model and the nominal controller output are set to the values calculated in the previous steps.

**8** Test controller performance and revise the design if necessary.

For example, the diagram below shows the model configured to test the response to a feed concentration of 9.5 kmol/m<sup>3</sup>. The nominal value is 10 kmol/m<sup>3</sup>



Run the Simulink model to obtain the trend plots shown below.



The decrease in feed concentration reduces heat generation. If the controller were absent, the reactor temperature would drop significantly, reducing the reduction rate, and the CSTR concentration would increase to roughly 3 kmol/m<sup>3</sup>. To counteract this, the controller raises the coolant temperature, returning the CSTR temperature to a value slightly below the nominal condition.

## **Testing an Existing Controller**

If you have already designed a model predictive controller to use with a Simulink plant, to test it in Simulink:

- 1 Open Simulink model.
- **2** Add an MPC Controller block to the model and connect it.
- **3** Specify the controller.

Open the MPC Controller and enter the name of your controller in the MPC Controller box. The string you enter here must be the name of an mpc object in the workspace.

**4** (Optional) Modify the controller.

To use mpctool, click **Design** with the MPC Controller open. Change the controller parameters and then export the modified controller to the workspace.

Alternatively, use commands to modify the controller object in the workspace.

5 Run the Simulink model.

### **Coordination of Multiple Model Predictive Controllers**

### In this section...

"A Two-Model Plant" on page 5-18

"Animation of the Multi-Model Example" on page 5-19

"Designing the Two Controllers" on page 5-21

"Simulating Controller Performance" on page 5-21

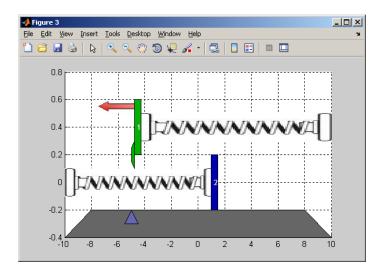
If your plant is nonlinear, a controller designed to operate in a particular target region may perform poorly in other regions. The common way to compensate is to design multiple controllers, each intended for a particular combination of operating conditions. Switch between them in real-time as conditions change. Gain scheduling is a conventional example of this technique. The following example shows how to coordinate multiple model predictive controllers for this purpose.

The rest of this section is an illustrative example organized as follows:

- "A Two-Model Plant" on page 5-18describes the example application involving two distinct operating conditions.
- "Animation of the Multi-Model Example" on page 5-19 explains how to simulate the plant.
- "Designing the Two Controllers" on page 5-21 shows how to obtain the controllers for each operating condition.
- "Simulating Controller Performance" on page 5-21 shows how to use the Multiple MPC Controllers block in Simulink to coordinate the two controllers.

### A Two-Model Plant

The figure below is a stop-action snapshot of the plant. It consists of two masses, M1 (upper) and M2 (lower). A spring connects M1 to a rigid wall and pulls it to the right. An applied force, shown as a red arrow, opposes the spring pulling M1 to the left.



In the above, mass M2 is uncontrollable. It responds solely to the spring pulling it to the left.

If the two masses collide, however, they stick together until a change in the applied force separates them.

The control objective is to make M1 track a reference signal. The blue triangle in the above indicates the desired location, which varies with time. At the instant shown, the desired numeric location is -5.

For an animated version of the plant, see Scheduling Controllers for a Plant with Multiple Operating Points.

### **Animation of the Multi-Model Example**

In order to achieve its objective, the controller can adjust the applied force magnitude (the length of the red arrow). It receives continuous measurements of the M1 location. There is also a contact sensor to signal collisions. The M2 location is unmeasured.

If M1 were isolated, this would be a routine control problem. The challenge is that the relationship between the applied force and M1's movement changes dramatically when M2 attaches to M1.

Define the model.

Define the system parameters.

```
M1 = 1; % mass
M2 = 5; % mass
k1 = 1; % spring constant
k2 = 0.1; % spring constant
b1 = 0.3; % friction coefficient
b2 = 0.8; % friction coefficient
yeq1 = 10; % wall mount position
yeg2 = -10; % wall mount position
```

Define a model of M1 when the masses are separated. Its states are the position and velocity of M1. Its inputs are the applied force, which will be the controller's manipulated variable (MV), and a spring constant calibration signal, which a measured disturbance (MD) input.

```
A1 = [0 1; -k1/M1 -b1/M1];
B1 = [0 \ 0; -1/M1 \ k1*yeq1/M1];
C1 = [1 \ 0];
D1 = [0 \ 0];
sys1 = ss(A1, B1, C1, D1);
sys1 = setmpcsignals(sys1, 'MV',1, 'MD',2);
```

The call to setmpcsignals specifies the input type for the two inputs.

Define another model (with the same input/output structure) to predict movement when the two masses are joined.

```
A2 = [0 1; -(k1+k2)/(M1+M2) -(b1+b2)/(M1+M2)];
B2 = [0 \ 0; -1/(M1+M2) \ (k1*veq1+k2*veq2)/(M1+M2)];
C2 = [1 \ 0];
D2 = [0 \ 0];
sys2 = ss(A2,B2,C2,D2);
sys2 = setmpcsignals(sys2,'MV',1,'MD',2);
```

### **Designing the Two Controllers**

Next, define controllers for each case. Both controllers employ a 0.2 second sampling period (Ts), a prediction horizon of p=20, a control horizon of m=1 and default values for all other controller parameters.

The only property that distinguishes the two controllers is the prediction model.

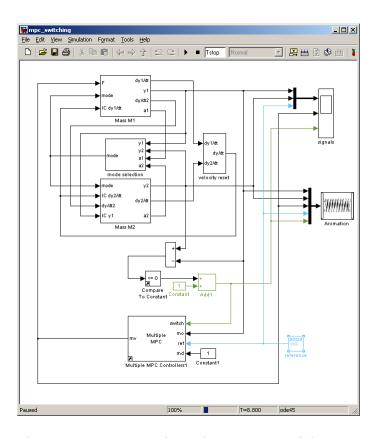
```
Ts = 0.2;
p = 20;
m = 1;
MPC1 = mpc(sys1,Ts,p,m); % Controller for M1 detached from M2
MPC2 = mpc(sys2,Ts,p,m); % Controller for M1 connected to M2
```

The applied force also have the same constraints in each case. The lower bound for the applied force is zero because it cannot reverse direction. The maximum rate of change for the applied force is 1000 per second (increasing or decreasing).

```
MPC1.MV = struct('Min',0,'RateMin',-1e3,'RateMax',1e3);
MPC2.MV = struct('Min',0,'RateMin',-1e3,'RateMax',1e3);
```

### **Simulating Controller Performance**

The following is the Simulink block diagram for this example.



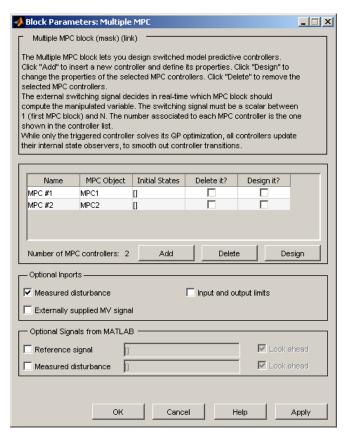
The upper portion simulates the movement of the two masses, plots the signals as a function of time and animates the plant.

The lower part contains the following key elements:

- A pulse generator that supplies the desired M1 position (the controller reference signal). The output of the pulse generator is a square wave that varies between —5 and 5, with a frequency of 0.015 per second.
- Simulation of a contact sensor. When the two masses have the same position, the Compare to Constant block evaluates to true and the Add1 block converts this to a 2. Else, the output of Add1 is 1.
- The Multiple MPC Controllers block, which has four inputs. The measured output (mo), reference (ref) and measured disturbance (md) inputs are as

for the MPC Controller block. The distinctive feature of the Multiple MPC Controllers block is the switch input.

The figure below shows the Multiple MPC Controllers block mask for this example.



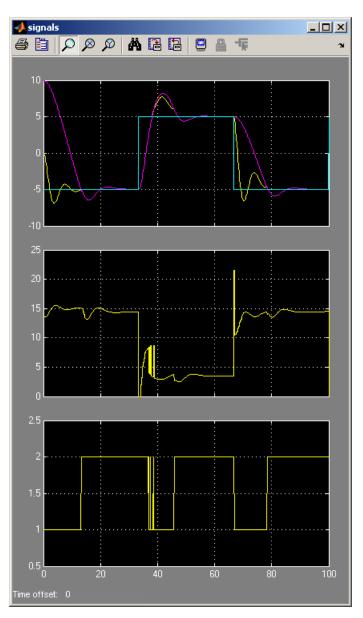
When the switch input is 1, the block automatically activates the first controller that is listed (MPC1), which is appropriate when the masses are separated. When the switch input is 2, the block automatically enables the second controller (MPC2).

Simulate the controller performance using Simulink commands.

```
Tstop = 100; % Simulation time
y1initial = 0; % Initial M1 and M2 Positions
```

```
y2initial = 10;
open('mpc_switching');
sim('mpc_switching',Tstop);
```

The figure below shows the signals scope output.



In the upper plot, the cyan curve is the desired position. It starts at -5. The M1 position (yellow) starts at 0. Under the control of MPC1, M1 moves

rapidly towards the desired position. M2 (magenta) starts at 10 and begins moving in the same direction.

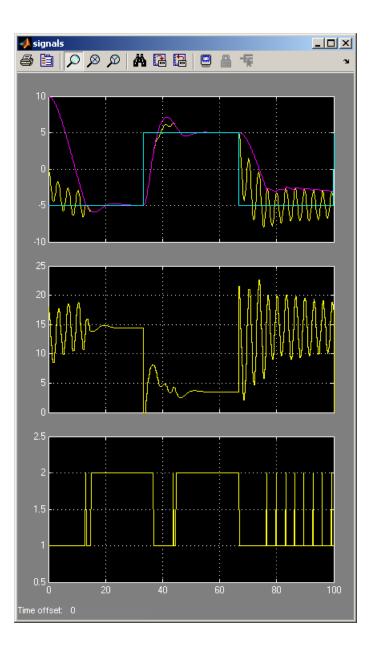
At about t = 13 seconds, M2 collides with M1. The switching signal (lower plot) changes at this instant from 1 to 2, so MPC2 takes over.

The completely inelastic collision moves M1 away from its desired position and M2 remains joined to M1. Controller MPC2 adjusts the applied force (middle plot) so M1 quickly returns to the desired position.

When the desired position changes step-wise to 5, the two masses separate briefly, with the controller switching to MPC1 appropriately. But, for the most part, the two masses move together and settle rapidly at the desired location. The transition back to —5 is equally well behaved.

Suppose we force MPC2 to operate under all conditions.

The figure below shows the result.



When the masses are disconnected, as at the start, MPC2 applies excessive force and then over-compensates, resulting in oscillatory behavior. Once the masses join, the move more smoothly, as would be expected.

The last transition causes especially severe oscillations. The masses collide frequently and M1 never reaches the desired position.

If MPC1 is in charge exclusively, the masses move sluggishly and fail to settle at the desired position before the next transition occurs. For more information, see the Scheduling Controllers for a Plant with Multiple Operating Points.

In this application, at least, two controllers are, indeed, better than one.

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